Physics 3922H Physics Colloquium Thur. 3.17.2016 Exercise Set 9 Solutions Due Thur 4.07 Read Unit 2 Chapter 4 (all) and Chapter 5 thru part (9).

1.In class<sup>†</sup> we constructed a quadratic dispersion  $(\upsilon, \kappa)$ -plot (frequency  $\upsilon vs$  wavenumber  $\kappa$ ) for the case of quadratic dispersion  $\upsilon = \kappa^2$ . The case involved a 1-CW (single coherent wave) with wavenumber  $(\upsilon = -1)$  colliding with another 1-CW of wavenumber  $(\upsilon = +2)$  and required you to derive and plot 2-CW (pair of interfering coherent waves) parameters of *frequencies*  $\upsilon_{Phase}^{2-CW}$  and  $\upsilon_{Group}^{2-CW}$  and *wavenumbers*  $\kappa_{Phase}^{2-CW}$ ,  $\kappa_{Group}^{2-CW}$ . With these we found wave velocities  $V_{Phase}^{2-CW}$  and  $V_{Group}^{2-CW}$ .

Now do this for the case of linear dispersion  $v = \kappa^1$  involving a 1-CW (single coherent wave) with wavenumber (v = -1) colliding with another 1-CW of wavenumber (v = +4). Use per-spacetime graph paper provided in class<sup>†</sup> to find 2-CW parameters  $v_{Phase}^{2-CW}$ ,  $v_{Group}^{2-CW}$ ,  $\kappa_{Group}^{2-CW}$ , and velocities  $V_{Phase}^{2-CW}$  and  $V_{Group}^{2-CW}$ . Make a table of the wave per-space-time parameters and (reciprocal) space-time ones as done in class.

2. The second part of the class<sup>†</sup> construction involved using the space-time 2-CW parameters that are reciprocals of  $v_{Phase}^{2-CW}$ ,  $v_{Group}^{2-CW}$ ,  $\kappa_{Group}^{2-CW}$ , namely periods  $\tau_{Phase}^{2-CW}$ ,  $\tau_{Group}^{2-CW}$  and wavelengths  $\lambda_{Phase}^{2-CW}$ ,  $\lambda_{Group}^{2-CW}$ .

Now do this for the case of linear dispersion  $v = \kappa^1$  (in part 1) and use the provided spacetime graph paper to plot and label a lattice for ideal 2-CW real-zeros in space and time. Label the line segments that correspond to periods and wavelengths as was done in class. Choose points so you make a symmetric array around origin (0,0) having at least 16 cells. Accuracy and neatness counts here. Precision should be to a fraction of the tiniest square on the graph.

<sup>†</sup> Class step-by-step constructions are in Lecture 22 ranging from p. 40 to around p.70. BohrIt animations in lecture show space-time lattices. First example is around p. 40.