

Assignment Set 1 - Read Unit 1 Ch. 1 thru Ch.3 - Due Tue. Aug. 29, 2017

Exercise 1 *Basic pool-shot kinetics*

Consider V_1 vs V_2 graphs for 1D-collisions between masses M_1 and M_2 described in Ch. 2 and Ch. 3.

Draw a graph of a collision with initial velocities $\mathbf{V}^{\text{IN}} = (V^{\text{IN}}_1, V^{\text{IN}}_2) = (0.5, 0.0)$ for equal masses ($M_1 = M_2 = 1$).

For a totally inelastic 'ka-runch' case derive final velocities $\mathbf{V}^{\text{FIN}} = (V^{\text{FIN}}_1, V^{\text{FIN}}_2)$ from graph and plot KE ellipse[†].

For a totally elastic 'ka-bong' case do the same. Compare final kinetic energy KE values for the two cases.

† At the end of Ch.3 is shown an easy ellipse construction given ellipse radii a and b . This should not be necessary for Exercise 1 but will come in handy for Exercise 2 below as will attached graph paper.

Exercise 2 *Head-on collision kinetics*

The full V_1 vs V_2 graphs for 1D-collisions of masses M_1 and M_2 described in Ch. 2 and Ch. 3 is needed here.

Solve using tensor algebraic methods and compare results to a geometric solution on graph paper given below.

Analyze collisions for initial velocities $\mathbf{V}^{\text{IN}} = (V^{\text{IN}}_1, V^{\text{IN}}_2) = (0.4, -0.2)$ for masses $M_1 = 5$ and $M_2 = 1$.

Derive final velocities $\mathbf{V}^{\text{FIN}} = (V^{\text{FIN}}_1, V^{\text{FIN}}_2) = \mathbf{V}^{\text{COM}}$ for a totally inelastic 'ka-runch' case.

Derive final velocities $\mathbf{V}^{\text{FIN}} = (V^{\text{FIN}}_1, V^{\text{FIN}}_2)$ for totally elastic 'ka-bong' case.

Derive $KE = \underline{\hspace{2cm}}$, KE -ellipse radii $a_1 = a \underline{\hspace{2cm}}$, $a_2 = b = \underline{\hspace{2cm}}$ for *ka-runch* case and construct its ellipse[†].

Derive $KE = \underline{\hspace{2cm}}$, KE -ellipse radii $a_1 = a \underline{\hspace{2cm}}$, $a_2 = b = \underline{\hspace{2cm}}$ for *ka-bong* case and construct its ellipse[†].

Derive $KE = \underline{\hspace{2cm}}$, KE -ellipse radii $a_1 = a \underline{\hspace{2cm}}$, $a_2 = b = \underline{\hspace{2cm}}$ for *ka-bong* case as viewed in COM frame.

Derive $KE = \underline{\hspace{2cm}}$, KE -ellipse radii $a_1 = a \underline{\hspace{2cm}}$, $a_2 = b = \underline{\hspace{2cm}}$ for *ka-runch* case as viewed in COM frame.

Construct resulting ellipse[†] for each case (if it exists).

Exercise 3 *Not-So-Head-on collision kinetics (Xtra credit)*

Analyze collisions for initial velocities $\mathbf{V}^{\text{IN}} = (V^{\text{IN}}_1, V^{\text{IN}}_2) = (0.4, +0.2)$ for masses $M_1 = 5$ and $M_2 = 1$.

Do geometric solution on graph paper given below

