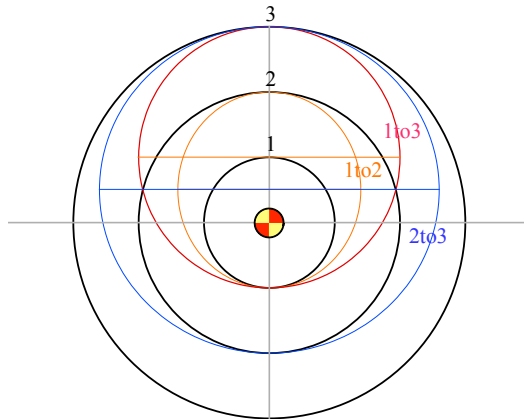**Revised** *Assignment 14* - **Physics 5103** 11/218/17 CMwBang Ch.5.1 to 5.3. and Lect.25-26 Due Thur. Dec. 7

Ex.1 *Two burns*

Space shuttle in circular orbit of radius R_1 uses two burns to transit to circular orbit of radius $R_n=nR_1$.
(a) Derive orbital parameters $(a,b,\varepsilon,\lambda)$ involved in transit 1to2, 2to3, and direct transit 1to3. Derive and plot focal points and latus radius and minor radius of each transit orbit. (Ellipses sketched above are a little too fat!)
(b) Find energy and angular momentum of each of five stages in terms of original energy E_1 and momentum L_1.
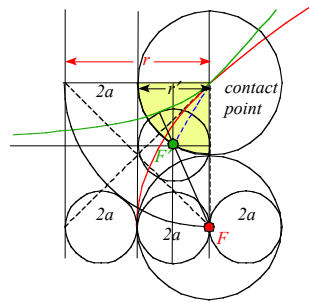
Ex.2 *Enveloping Rutherford's Coulomb orbits*

This exercise mostly concerns α^{++} orbits repelled by positively charged nucleus but also considers anti-α^{--} orbits attracted to the nucleus.
(a) By ruler&compass geometry construct Rutherford orbits of radius $a=1$ for impact parameter $b=2$ and $b=4$. Show left-incoming and upper-right-outgoing asymptotes and their scattering angles. Check angle geometry algebraically. Be sure to include axis lines containing atomic nuclear focal point F, orbit center C, and 2nd focus F″ for each orbit. First find what b-value makes α^{++} fly away at $\Phi=90°$ to beam.
Hint: Geometry of forward scattering half-angle $\Phi/2$ is simpler since its center is nucleus point F that is center of protractor graph paper.
(b) Each repelling α^{++} orbit has a symmetric attracting α^{--} orbit on the other side. Draw their paths and asymptotes.
(c) On a separate graph superimpose the repelling orbits of **(a)** and use their geometry to help derive the locus of the Rutherford scattering caustic that is the contact envelope of all repelling alpha paths for a given a. Describe how to locate a contact point for a given b-trajectory with the a-envelope. Is F ever a contact point?
Hints: Envelope geometry uses "kite" structure of parabolic tangents.
Recall that contact point always shares a line with focal point of envelope and focal point of contacting curve.
(d) Could Rutherford's alpha beams conceivably osculate (kiss) the nucleus? That is, could the contact envelope ever match and meet the curvature of the nucleus itself?
(e) How many eV of energy does an α^{+4} particle need to touch a Au^{+79} nucleus with an assumed radius $r= 1fm$? Discuss how possible it is that Rutherford may have been able to accomplish this. ($1eV=1.6·10^{-19}Joule$. Gold has 79 protons while each α^{++} has just two, each with charge $1.6·10^{-19}Coulomb$ equal in magnitude to that of the electron. Highest energy alpha emitter is *Astatine-217* with *7.067MeV*.)

F