

AMOP Lectures 6.0

Tue 2.18 2014

Introduction to Relativistic Classical and Quantum Mechanics I.

(Ch. 2-5 of Unit 8)

Review of group velocity vs. phase velocity and tangent contacts

“Sin-Tan” geometry in “Relativity” (www.uark.edu/ua/modphys/testing/markup/RelaWavityWeb.html)

“Sinh-Tanh” geometry

“Per-Space-Time” geometry

The rare case where group velocity is both $\Delta\omega/\Delta k$ and $d\omega/dk$

How optical CW group and phase properties give relativistic mechanics

What’s the Matter with Mass?

Brief look at Higgs

Three kinds of mass (Einstein rest mass, Galilean momentum mass, Newtonian inertial mass)

What’s the matter with light?

Bohr-Schrodinger (BS) approximation throws out Mc^2

Relativistic Classical and Quantum Mechanics

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"Sin-Tan Rosetta"

Sin-Tan Rosetta

Transistion to Hyperbolic

Controls

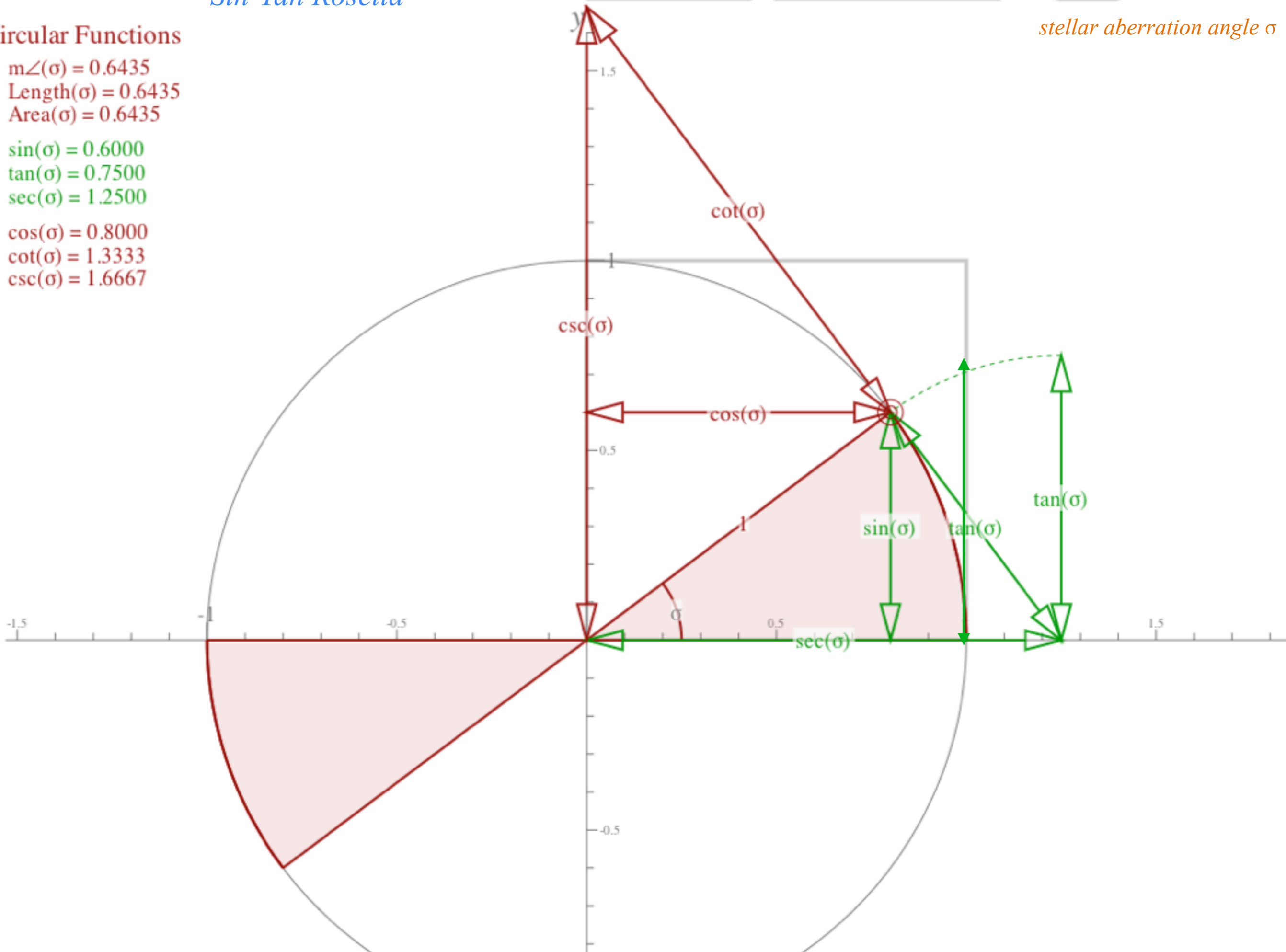
Circular Functions

$m\angle(\sigma) = 0.6435$
 $\text{Length}(\sigma) = 0.6435$
 $\text{Area}(\sigma) = 0.6435$

$\sin(\sigma) = 0.6000$
 $\tan(\sigma) = 0.7500$
 $\sec(\sigma) = 1.2500$

$\cos(\sigma) = 0.8000$
 $\cot(\sigma) = 1.3333$
 $\csc(\sigma) = 1.6667$

stellar aberration angle σ



"Sin-Tan Rosetta"

Sin-Tan Rosetta

Transition to Hyperbolic

Controls

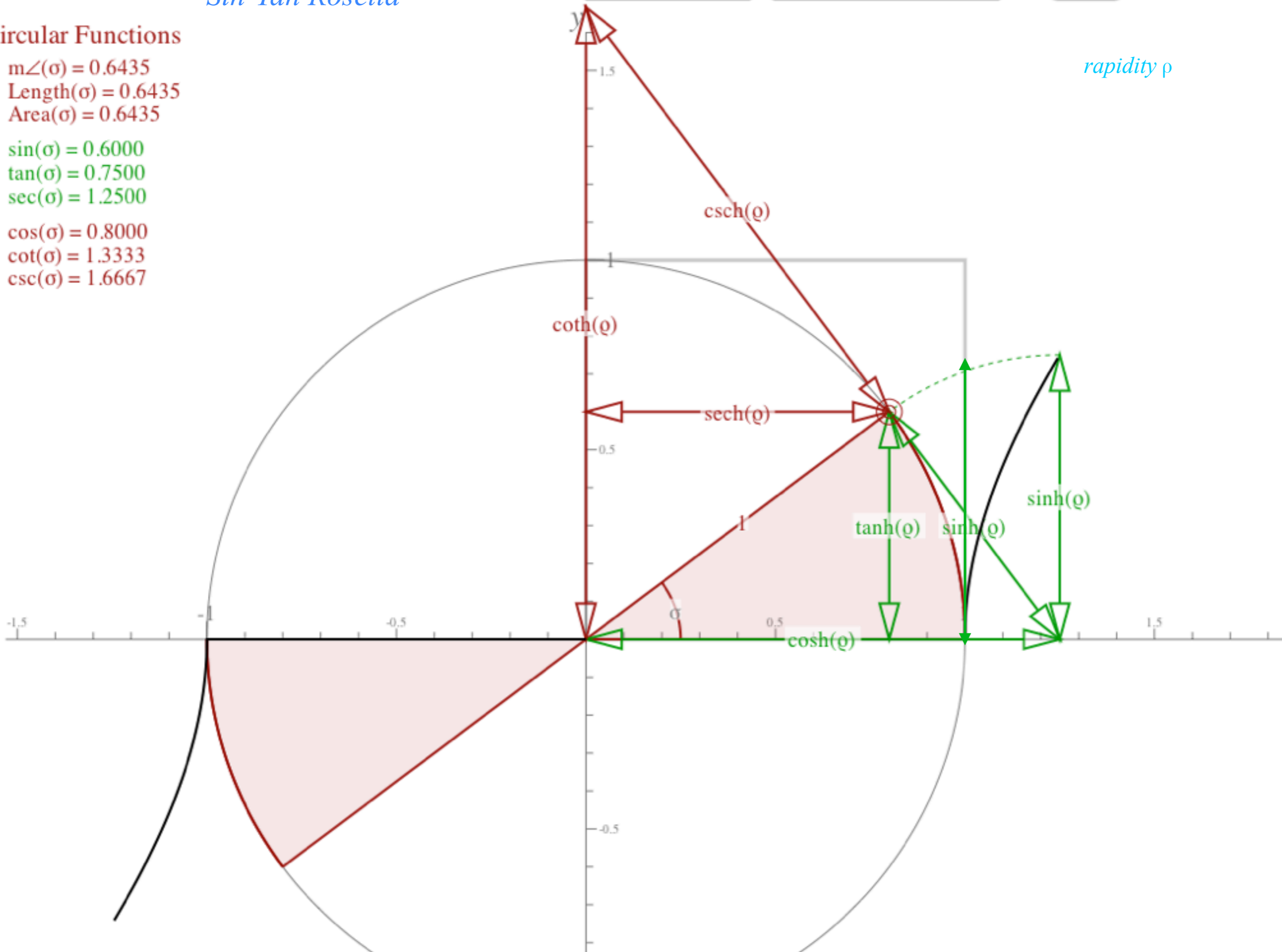
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rapidity ρ



"Sin-Tan Rosetta"

Sin-Tan Rosetta

Transition to Hyperbolic

Controls

Circular Functions

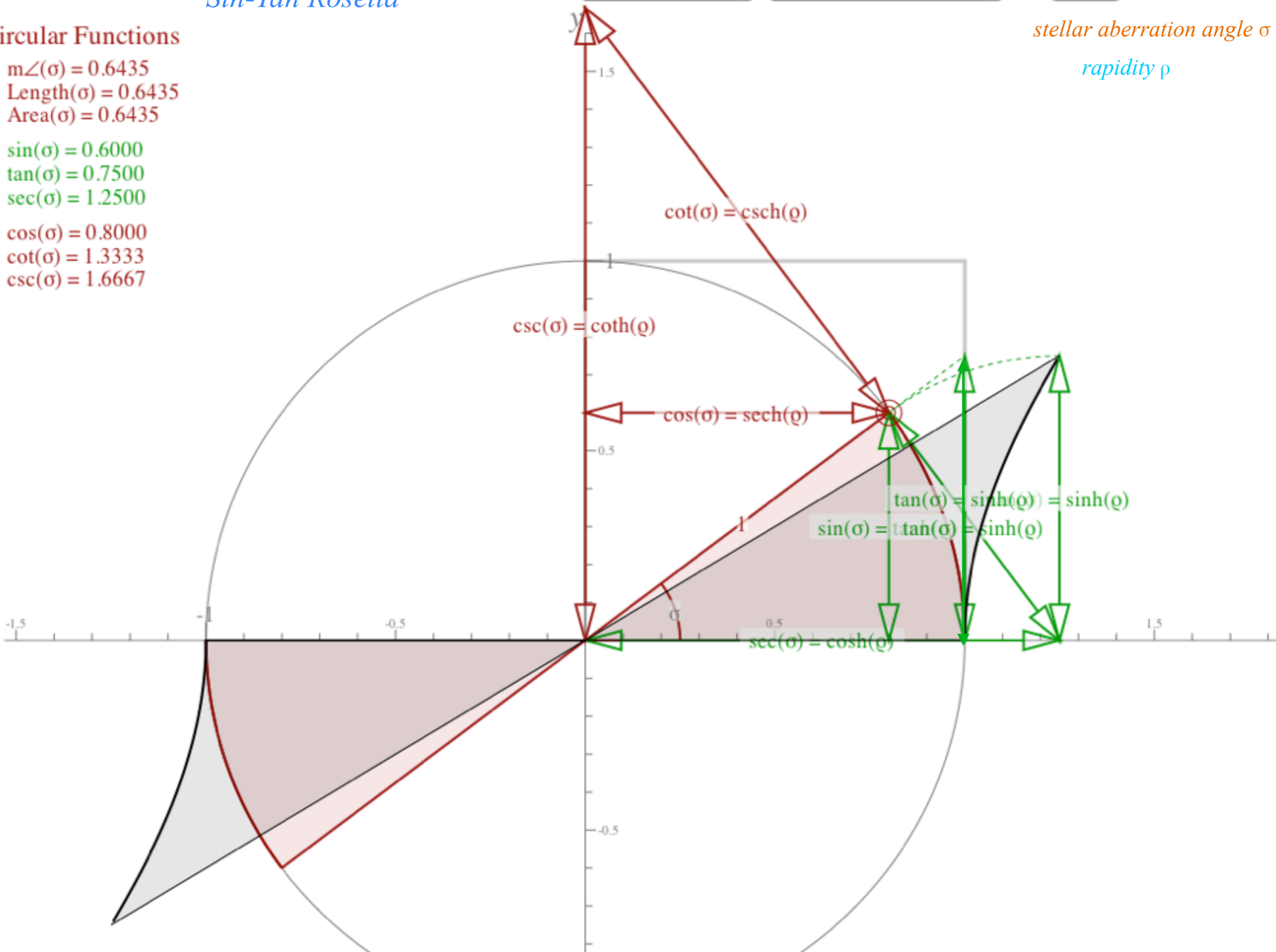
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stellar aberration angle σ

rapidity ρ



"Sin-Tan Rosetta"

Sin-Tan Rosetta

Transition to Hyperbolic

Controls

Circular Functions

Hyperbolic Functions

$m\angle(\sigma) = 0.6435$
 Length(σ) = 0.6435
 Area(σ) = 0.6435

$\rho = 0.6931$
 Area(ρ) = 0.6931

$\sin(\sigma) = 0.6000$
 $\tan(\sigma) = 0.7500$
 $\sec(\sigma) = 1.2500$

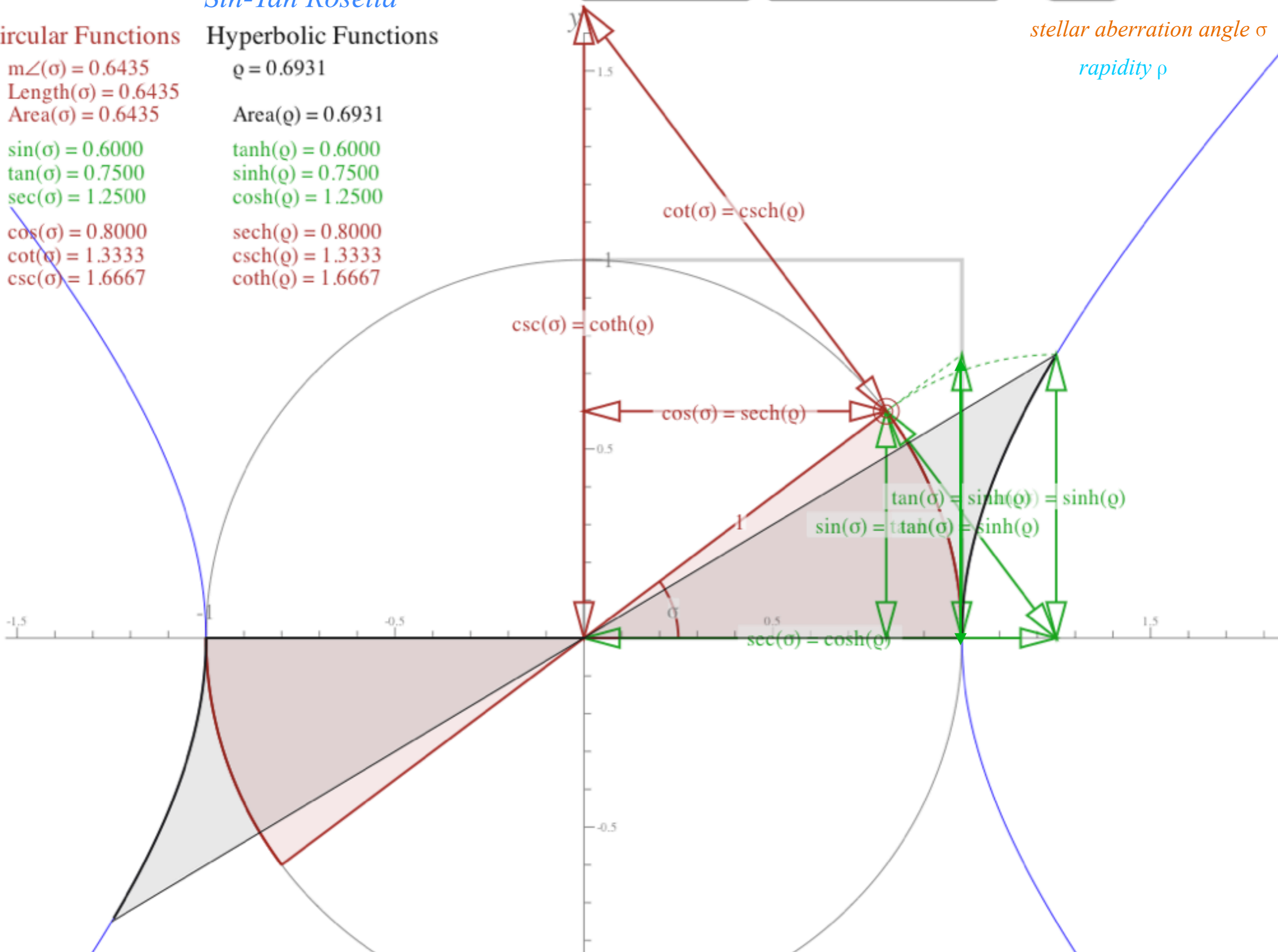
$\tanh(\rho) = 0.6000$
 $\sinh(\rho) = 0.7500$
 $\cosh(\rho) = 1.2500$

$\cos(\sigma) = 0.8000$
 $\cot(\sigma) = 1.3333$
 $\csc(\sigma) = 1.6667$

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stellar aberration angle σ

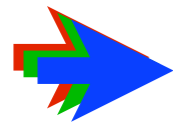
rapidity ρ



Relativistic Classical and Quantum Mechanics

Review of group velocity vs. phase velocity and tangent contacts

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“Sinh-Tanh” geometry

“Per-Space-Time” geometry

The rare case where group velocity is both $\Delta\omega/\Delta k$ and $d\omega/dk$

The "Sinh-Tanh Rosetta"

Sinh-Tanh Rosetta

All

Controls

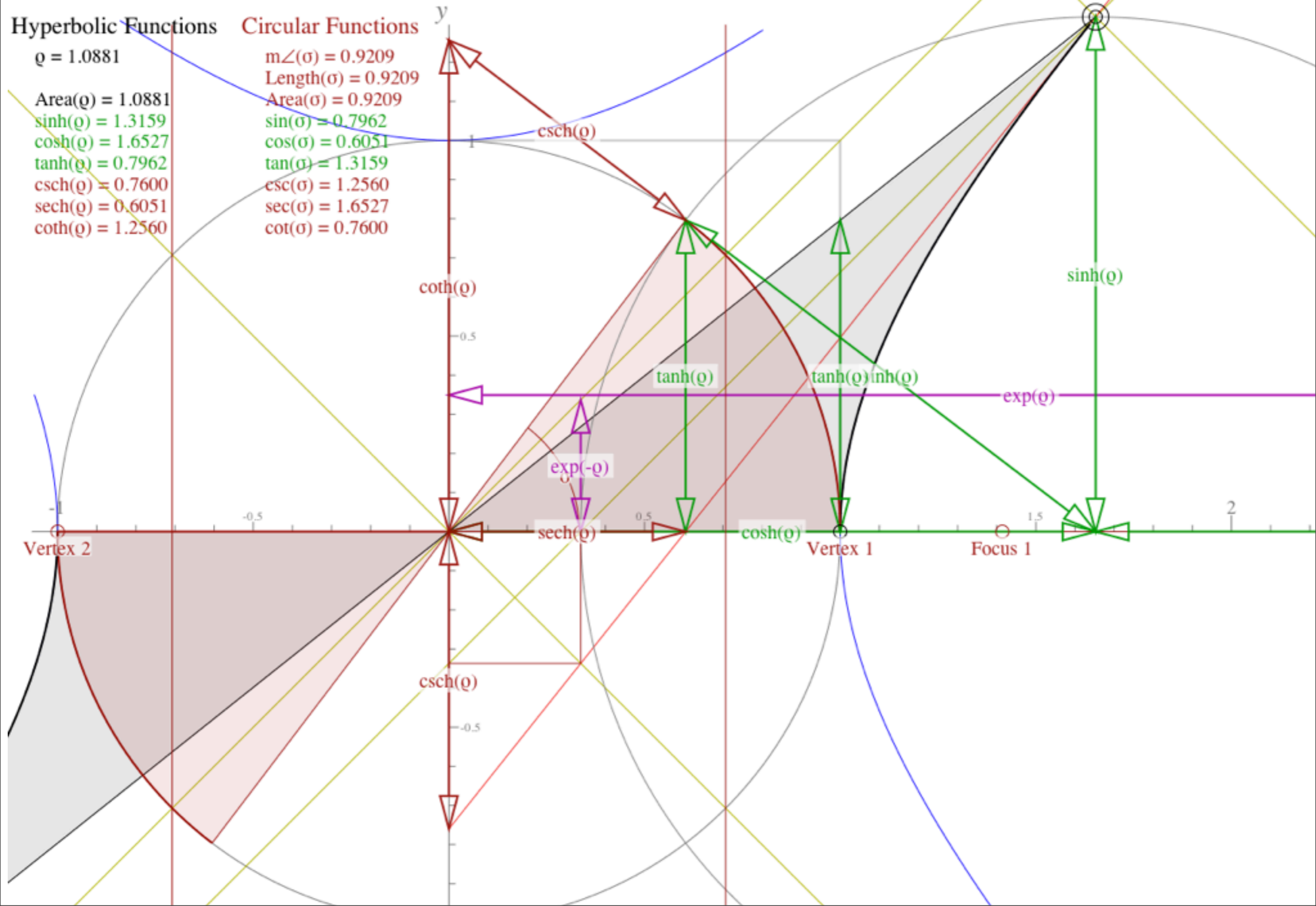
rapidity ρ

Hyperbolic Functions

Circular Functions

$\rho = 1.0881$
 Area(ρ) = 1.0881
 sinh(ρ) = 1.3159
 cosh(ρ) = 1.6527
 tanh(ρ) = 0.7962
 csch(ρ) = 0.7600
 sech(ρ) = 0.6051
 coth(ρ) = 1.2560

$m\angle(\sigma) = 0.9209$
 Length(σ) = 0.9209
 Area(σ) = 0.9209
 sin(σ) = 0.7962
 cos(σ) = 0.6051
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Relativistic Classical and Quantum Mechanics

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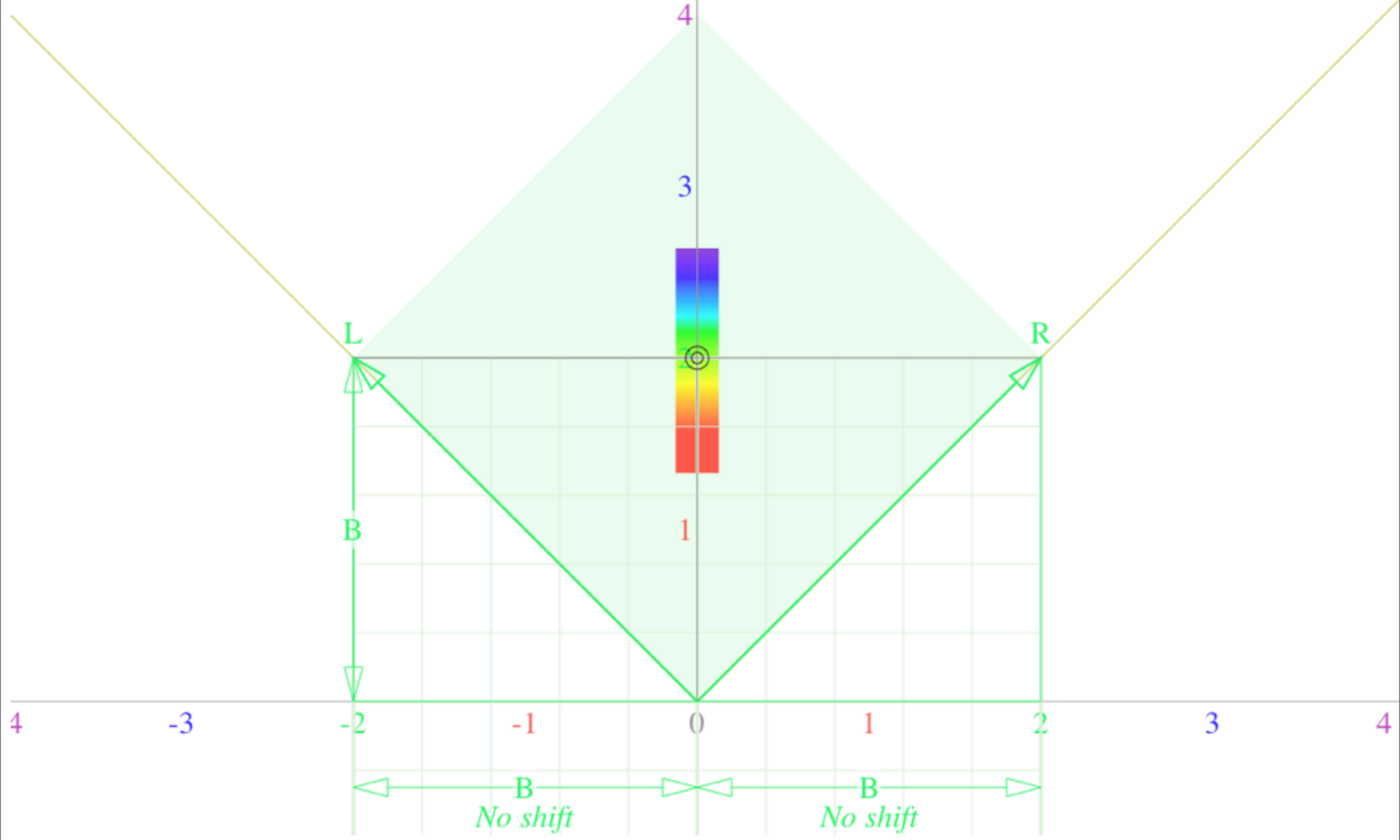
“Sinh-Tanh” geometry



“Per-Space-Time” geometry

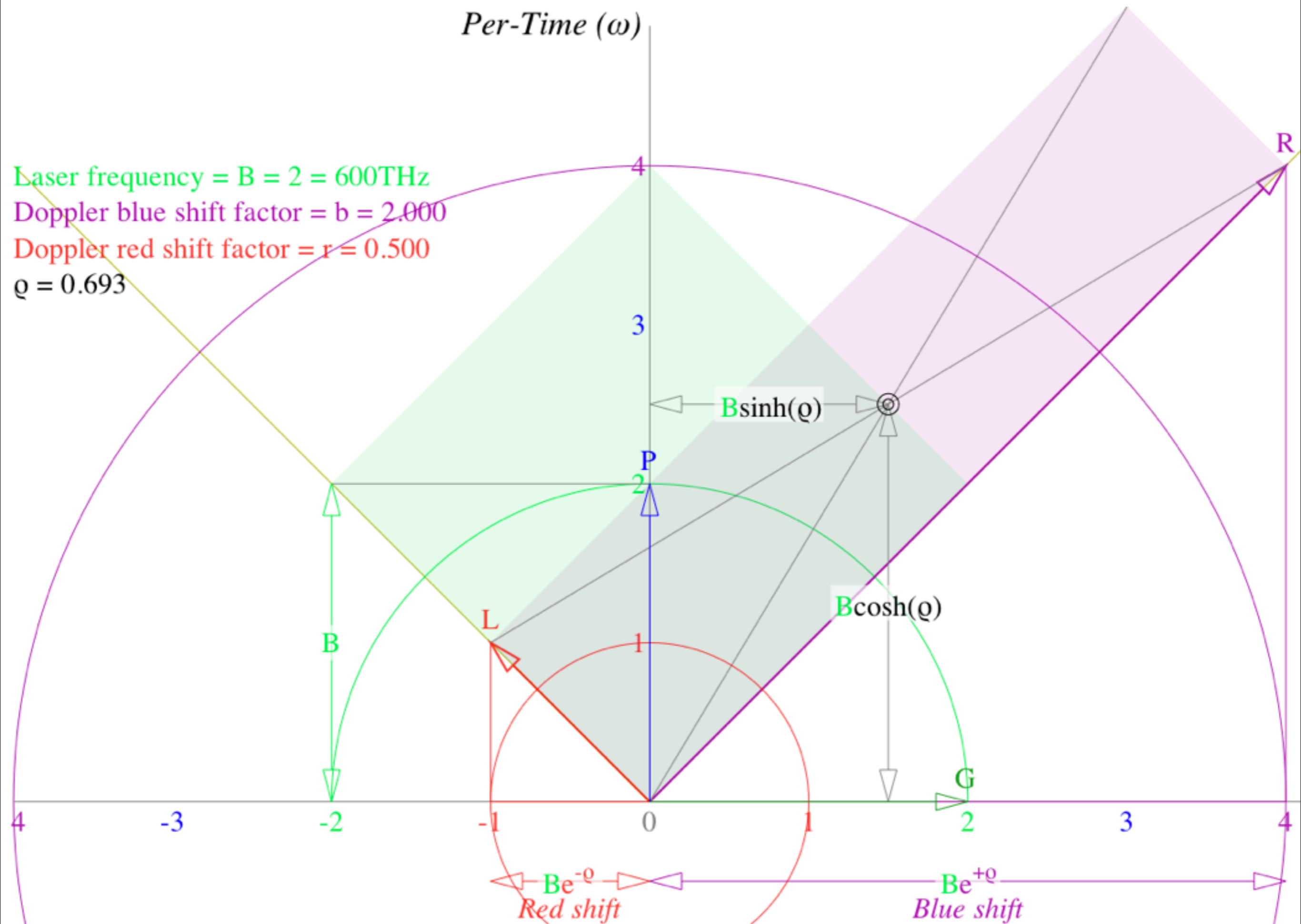
The rare case where group velocity is both $\Delta\omega/\Delta k$ and $d\omega/dk$

Per-Time (ω)



Per-Time (ω)

Laser frequency = $B = 2 = 600\text{THz}$
 Doppler blue shift factor = $b = 2.000$
 Doppler red shift factor = $r = 0.500$
 $q = 0.693$



Per-Time (ω)

Laser frequency = $B = 2 = 600\text{THz}$
 Doppler blue shift factor = $b = 2.000$
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 $\varrho = 0.693$

$$B \cosh(\varrho) = (B e^{+\varrho} + B e^{-\varrho})/2$$

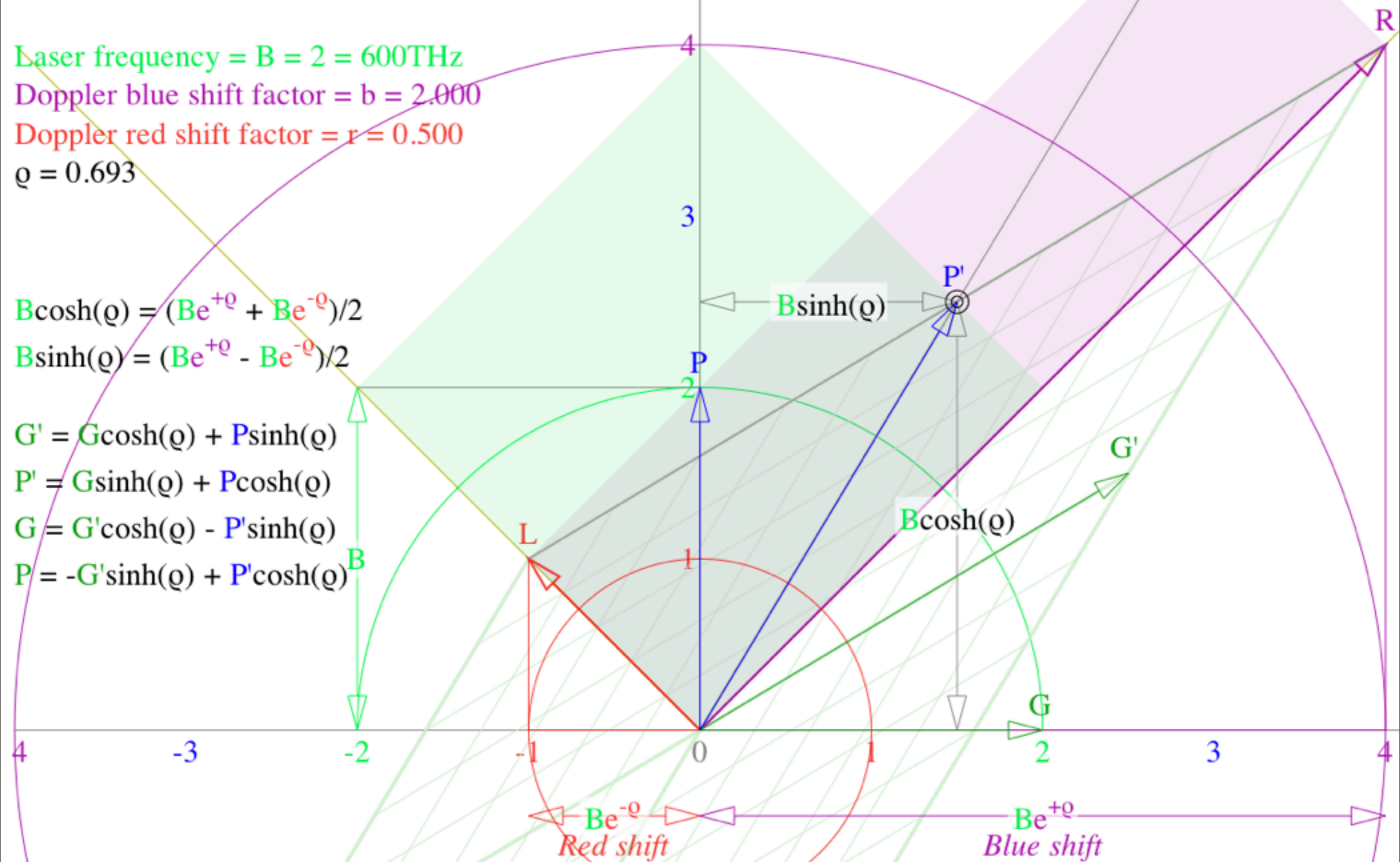
$$B \sinh(\varrho) = (B e^{+\varrho} - B e^{-\varrho})/2$$

$$G' = G \cosh(\varrho) + P \sinh(\varrho)$$

$$P' = G \sinh(\varrho) + P \cosh(\varrho)$$

$$G = G' \cosh(\varrho) - P' \sinh(\varrho)$$

$$P = -G' \sinh(\varrho) + P' \cosh(\varrho)$$



$B e^{-\varrho}$
Red shift

$B e^{+\varrho}$
Blue shift

Per-Time (ω)

Laser frequency = $B = 2 = 600\text{THz}$
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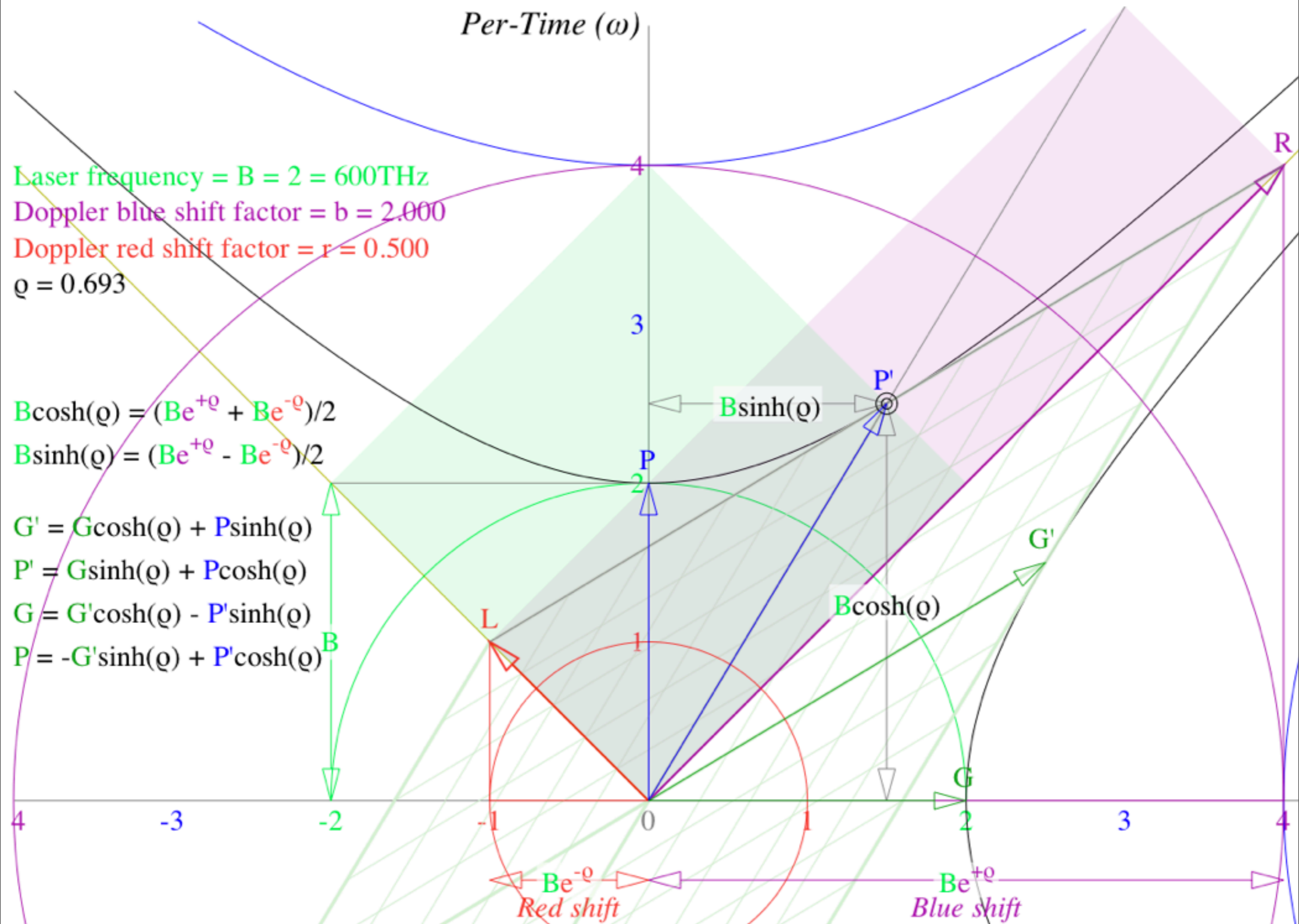
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Per-Time (ω)

Laser frequency = $B = 2 = 600\text{THz}$
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$$B\cosh(q) = (Be^{+q} + Be^{-q})/2$$

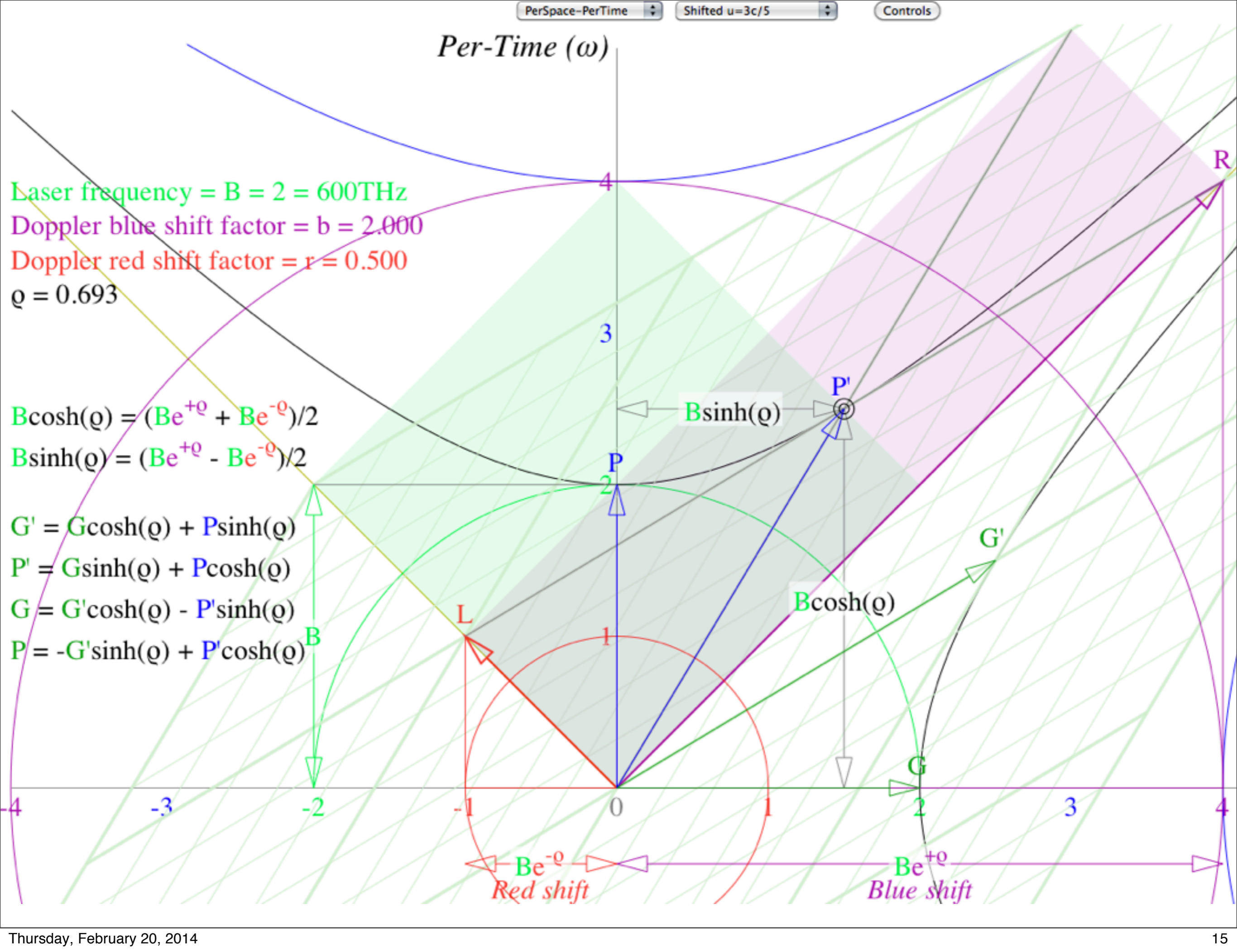
$$B\sinh(q) = (Be^{+q} - Be^{-q})/2$$

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$$G = G'\cosh(q) - P'\sinh(q)$$

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Be^{-q}
Red shift

Be^{+q}
Blue shift

Per-Time (ω)

time	r_{Dopp}	v_{group}	τ_{phase}	v_{phase}	τ_{group}	b_{Dopp}	u/c	c/u
space		κ_{phase}	λ_{group}	κ_{group}	λ_{phase}		V_{group}/c	V_{phase}/c
rapidity ρ	$e^{-\rho}$	$\sinh \rho$	$\operatorname{sech} \rho$	$\cosh \rho$	$\operatorname{csch} \rho$	$e^{+\rho}$	$\tanh \rho$	$\operatorname{coth} \rho$
stellar $\nabla \sigma$		$\tan \sigma$	$\cos \sigma$	$\sec \sigma$	$\cot \sigma$		$\sin \sigma$	$\csc \sigma$
QM		p	$-L$	H	λ_{DeB}		$d\omega/dk$	ω/k
Old Fashioned Formulas	$\sqrt{\frac{1+u/c}{1-u/c}}$	$\frac{1}{\sqrt{1-u^2/c^2}}$	$-\sqrt{1-u^2/c^2}$	$\frac{1}{\sqrt{1-u^2/c^2}}$	$\sqrt{1-u^2/c^2}$	$\sqrt{\frac{1+u/c}{1-u/c}}$	$\frac{u}{c}$	$\frac{c}{u}$

Laser frequency = $B = 2 = 600\text{THz}$
 Doppler blue shift factor = $b = 2.000$
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 $\rho = 0.693$

$B \cosh(\rho) = (Be^{+\rho} + Be^{-\rho})/2$

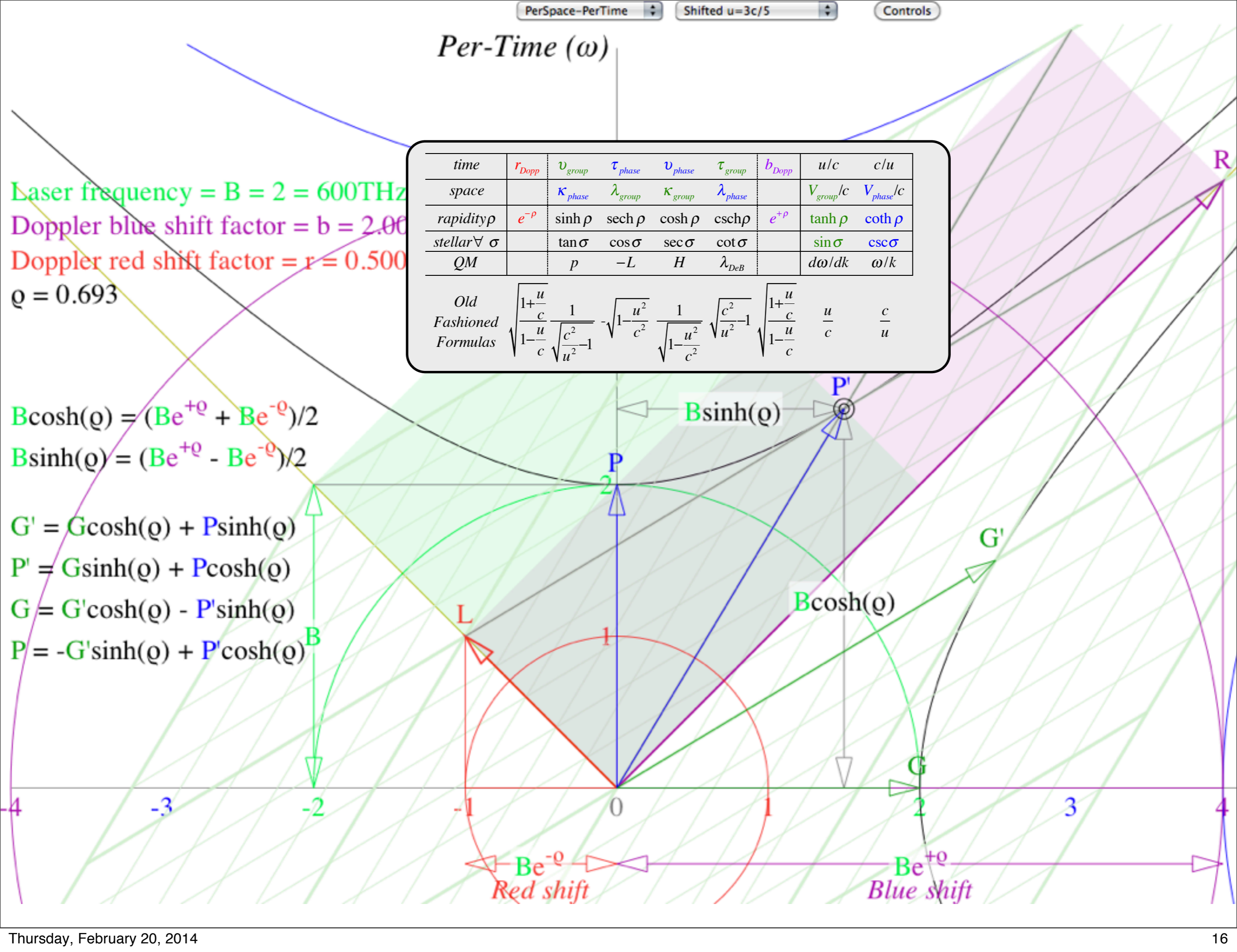
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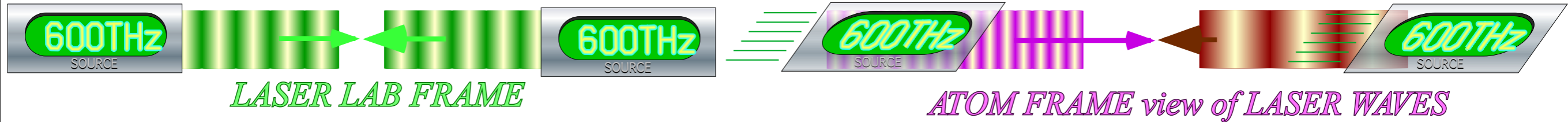
$P = -G' \sinh(\rho) + P' \cosh(\rho)$



$Be^{-\rho}$
Red shift

$Be^{+\rho}$
Blue shift

Per-space-time has Minkowski coordinates, too!



atom speed $-u$
LaserPer-Spacetime

atom speed 0
AtomPer-Spacetime

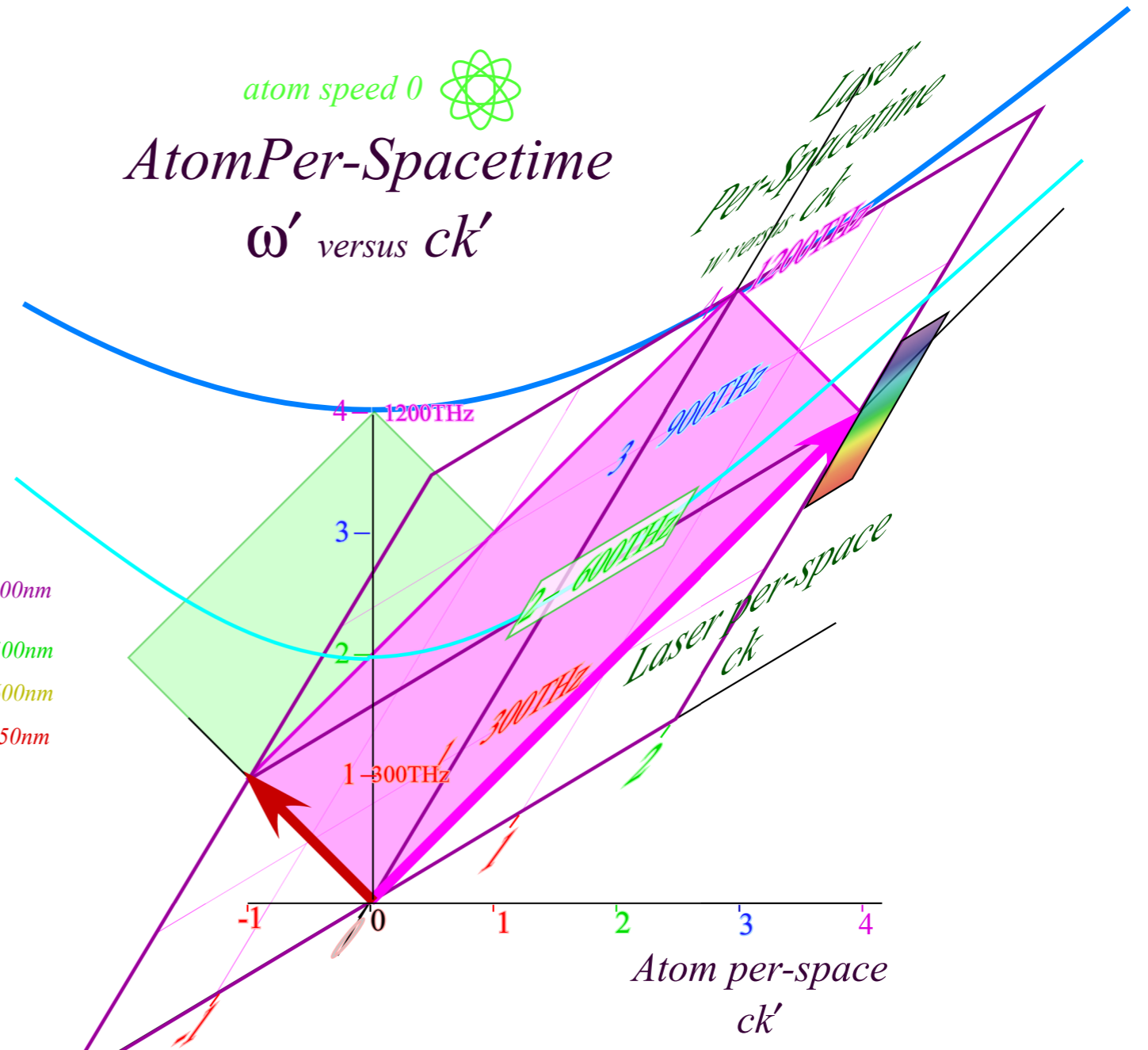
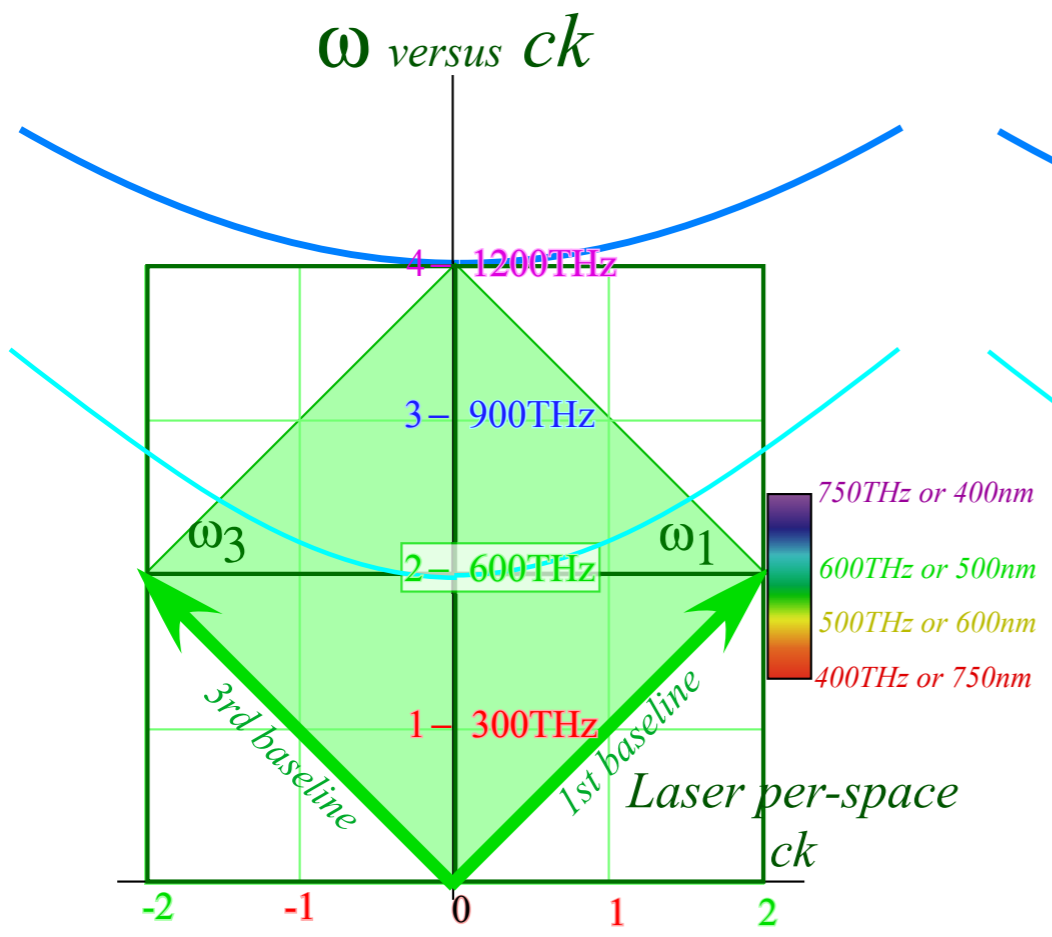


Fig. 8.3.5 Dispersion hyperbolas for 2-CW interference (a) Laser lab view. (b) Atom frame view.

*Fig. 3.5 from
 CMwBang!
 Ch. 3 of Unit 8.*

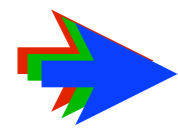
Relativistic Classical and Quantum Mechanics

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The rare case where group velocity is both $\Delta\omega/\Delta k$ and $d\omega/dk$

Group velocity u and phase velocity c^2/u
are hyperbolic tangent slopes

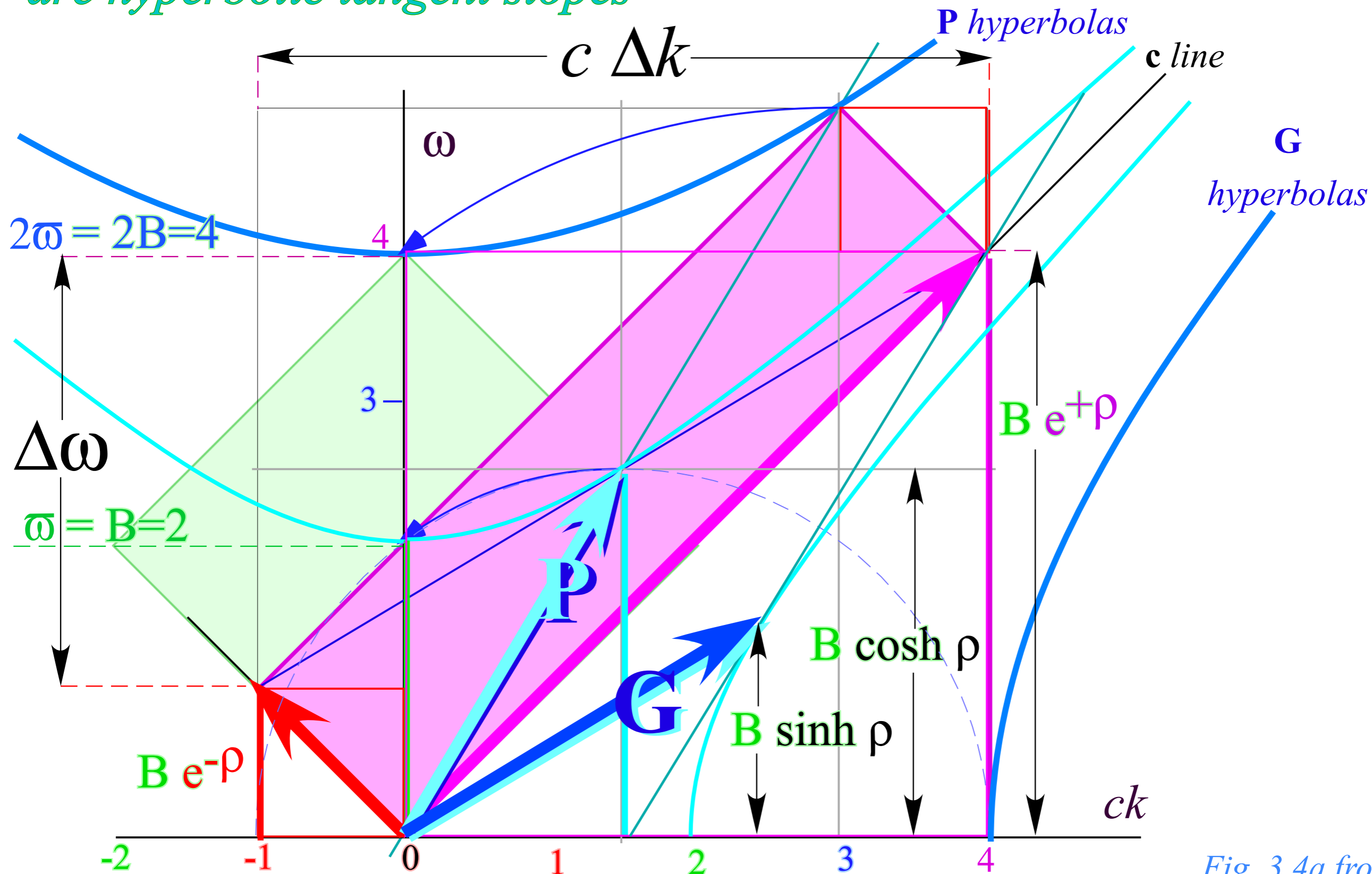


Fig. 3.4a from
CMwBang!
Ch. 3 of Unit 8.

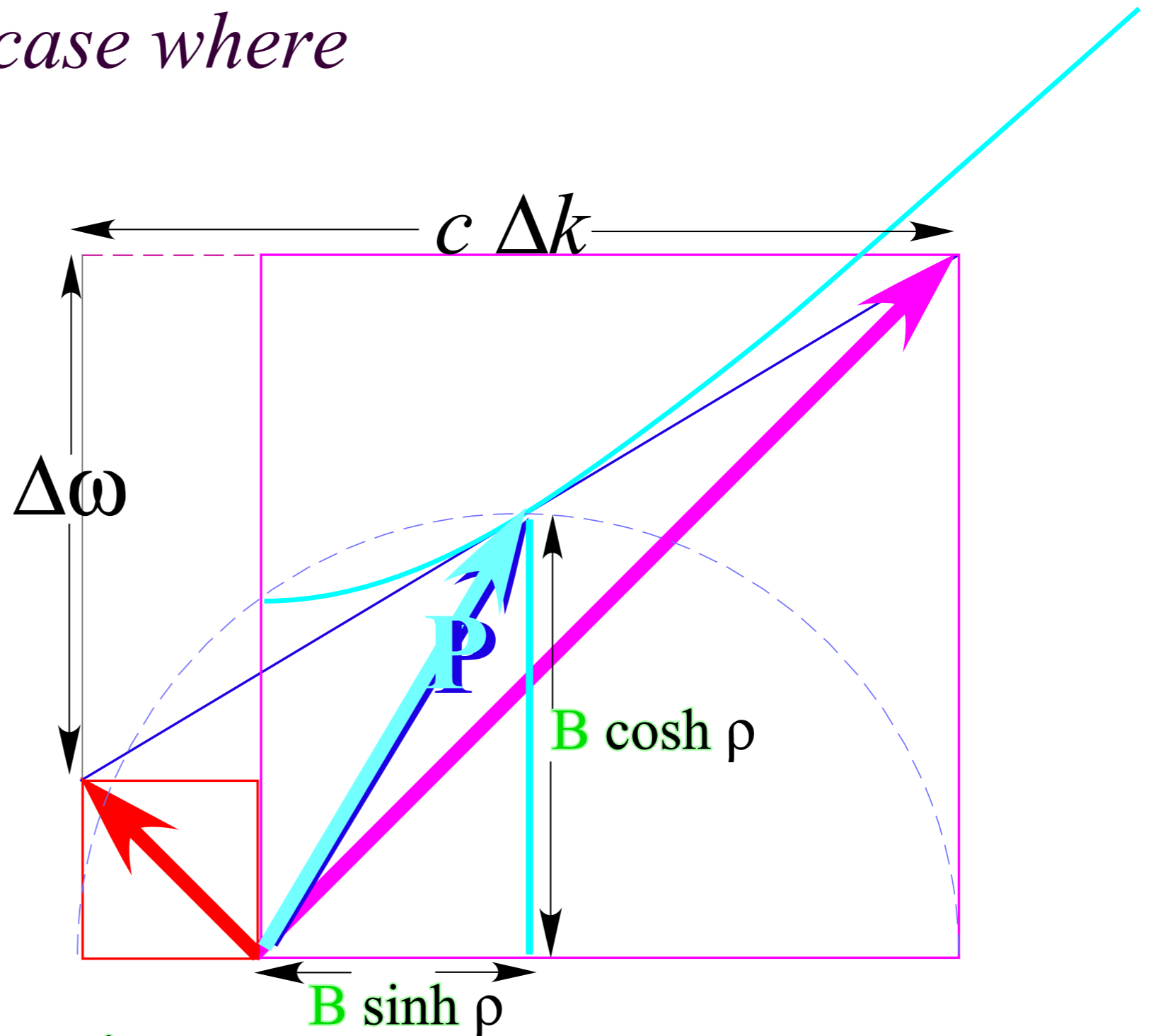
*Group velocity u and phase velocity c^2/u
are hyperbolic tangent slopes*

Rare but important case where

$$\frac{d\omega}{dk} = \frac{\Delta\omega}{\Delta k}$$

*with LARGE Δk
(not infinitesimal)*

*Relativistic
group wave
speed $u = c \tanh \rho$*



Low speed approximation

Newtonian speed $u \sim c\rho$

Rapidity ρ approaches u/c

Group velocity u and phase velocity c^2/u are hyperbolic tangent slopes

$$\frac{\omega}{ck} = \frac{c}{u}$$

Phase velocity

Group velocity

$$\frac{d\omega}{dck} = \frac{u}{c} = \frac{ck}{\omega}$$

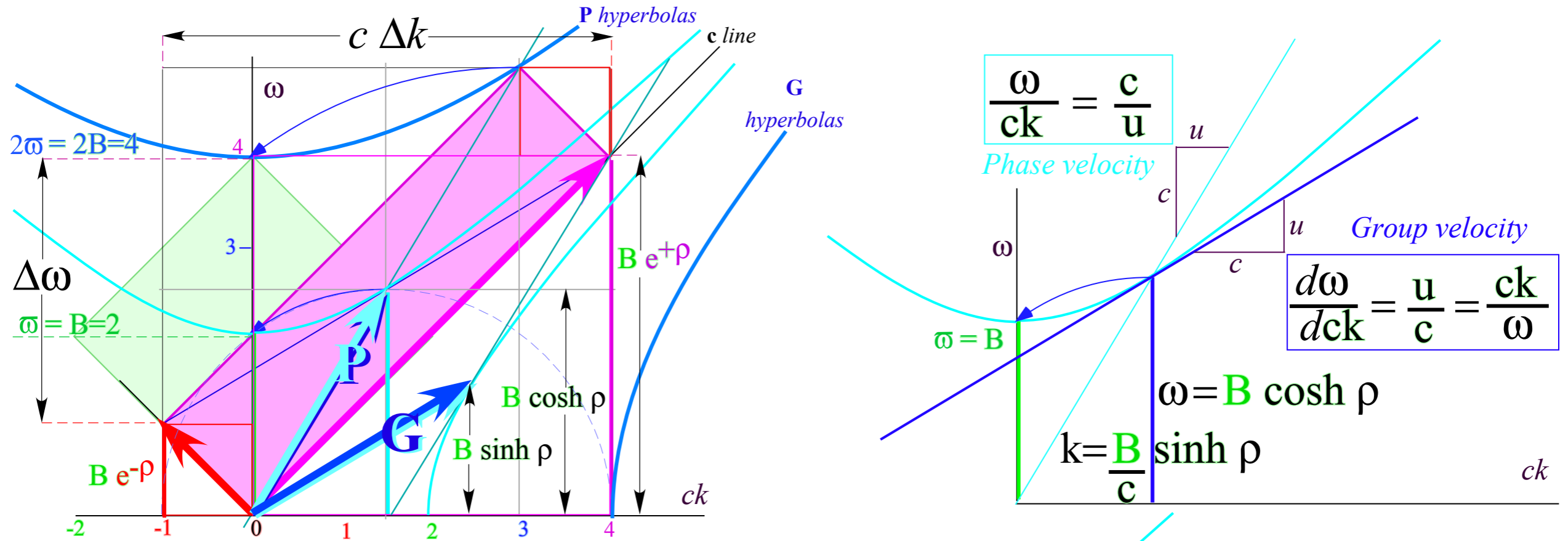
$$\omega = B \cosh \rho$$

$$k = \frac{B}{c} \sinh \rho$$

ck

Group velocity u and phase velocity c^2/u are hyperbolic tangent slopes

Fig. 3.4 from
CMwBang!
Ch. 3 of Unit 8.

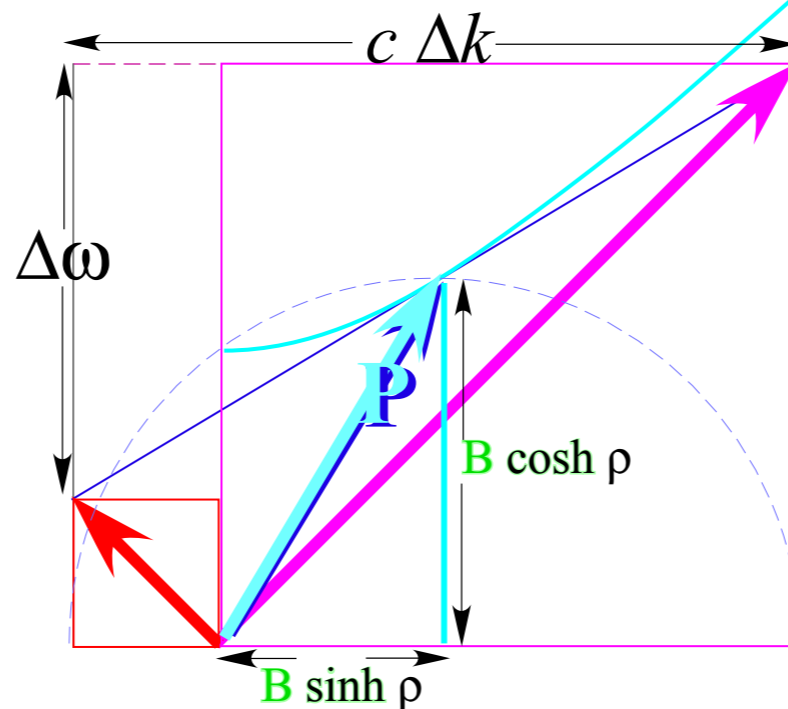


Rare but important case where

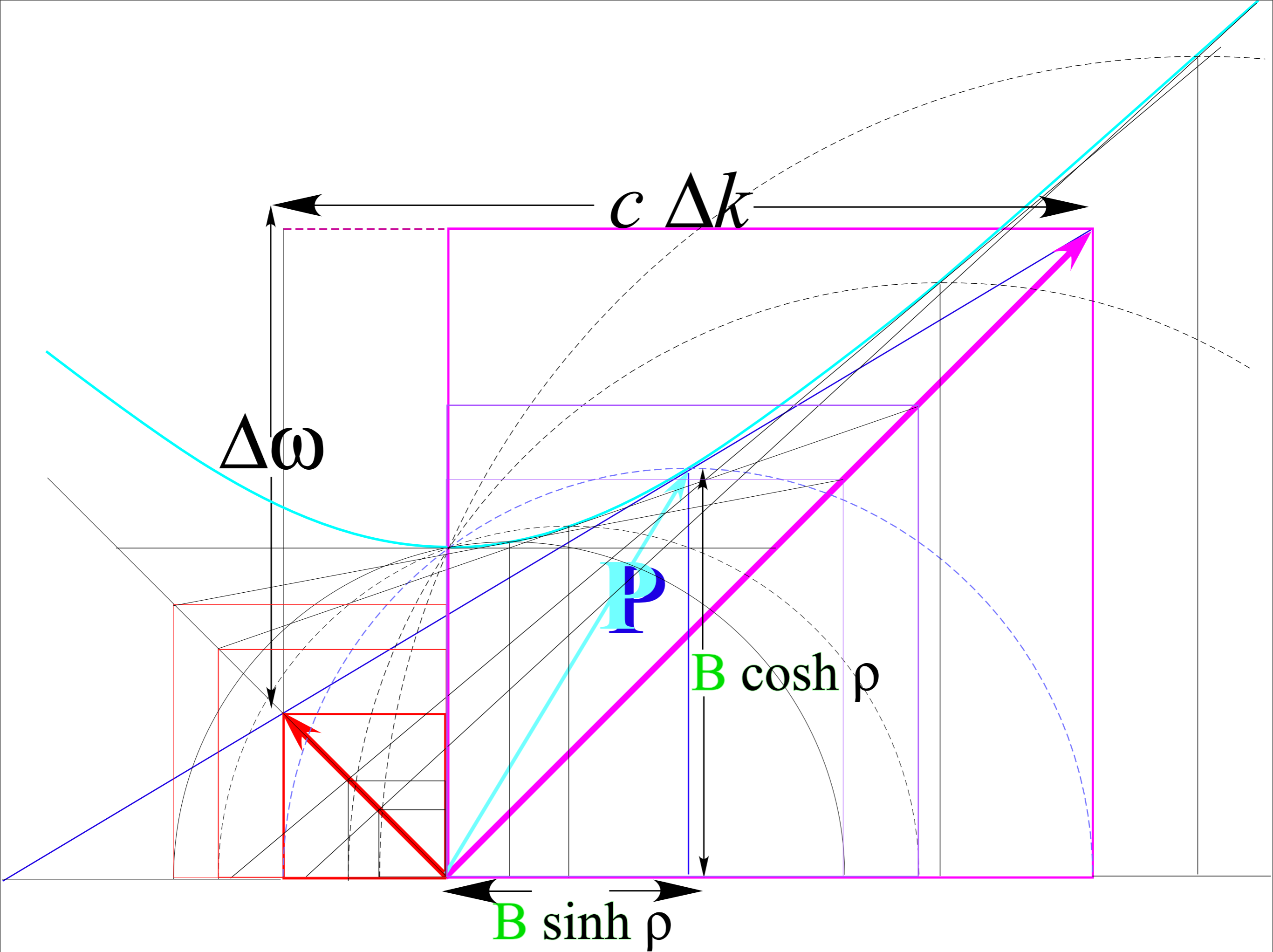
$$\frac{d\omega}{dk} = \frac{\Delta\omega}{\Delta k}$$

with **LARGE** Δk
(not infinitesimal)

Relativistic
group wave
speed $u = c \tanh \rho$



Newtonian speed $u \sim c\rho$
Low speed approximation
Rapidity ρ approaches u/c



Relativistic Classical and Quantum Mechanics

 *How optical CW group and phase properties give relativistic mechanics*

What's the Matter with Mass?

Brief look at Higgs

Three kinds of mass (Einstein rest mass, Galilean momentum mass, Newtonian inertial mass)

What's the matter with light?

Bohr-Schrodinger (BS) approximation throws out Mc^2

Start with low speed approximations : $\omega = B \cosh \rho = B(1 + \frac{1}{2} \rho^2 + \dots)$ where: $\rho \approx \frac{u}{c}$

CW Axioms (“All colors go c.” and “ $r=1/b$ ”) imply hyperbolic dispersion then mechanics of matter

$$\omega = B \cosh \rho \cong B + \frac{1}{2} \frac{B}{c^2} u^2$$

These follow from
CW axioms

$$k = \frac{B}{c} \sinh \rho \cong \frac{B}{c^2} u$$

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These follow from CW axioms

$$k = \frac{B}{c} \sinh \rho \approx \frac{B}{c^2} u$$

$$E = \text{constant} + \frac{1}{2} M u^2$$

(Newton's energy)

$$p = M u$$

(Galileo's momentum)

So 2-CW-light frequency ω is like **energy** E while k -number is like **momentum** p ,

Start with low speed approximations : $\omega = B \cosh \rho = B(1 + \frac{1}{2}\rho^2 + \dots)$ where: $\rho \approx \frac{u}{c}$

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So 2-CW-light frequency ω is like **energy** E while k -number is like momentum p , implies Planck's $E = s \cdot \omega$ scaling with factors: $s = \hbar = s$ equal to DeBroglie's $p = s \cdot k$.

$$E = s \omega = s B \cosh \rho \approx s B + \frac{1}{2} \frac{s B}{c^2} u^2$$

$$p = s k = \frac{s B}{c} \sinh \rho \approx \frac{s B}{c^2} u$$

Start with low speed approximations : $\omega = B \cosh \rho = B(1 + \frac{1}{2}\rho^2 + \dots)$ where: $\rho \approx \frac{u}{c}$

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$$p = s k = \frac{s B}{c} \sinh \rho \approx \frac{s B}{c^2} u$$

Both relations imply: $M = \frac{s B}{c^2}$ giving a (famous) *rest energy constant* : $s B = M c^2$

This then gives the famous *Einstein energy* E and also the *Einstein momentum* p

CW Axioms (“All colors go c.” and “ $r=1/b$ ”) imply hyperbolic dispersion then mechanics of matter

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This then gives the famous Einstein energy E and also the Einstein momentum p

$$E = s \omega = M c^2 \cosh \rho \cong M c^2 + \frac{1}{2} M u^2$$

$$p = s k = M c \sinh \rho \cong M u$$

$$= \frac{M c^2}{\sqrt{1 - u^2/c^2}}$$

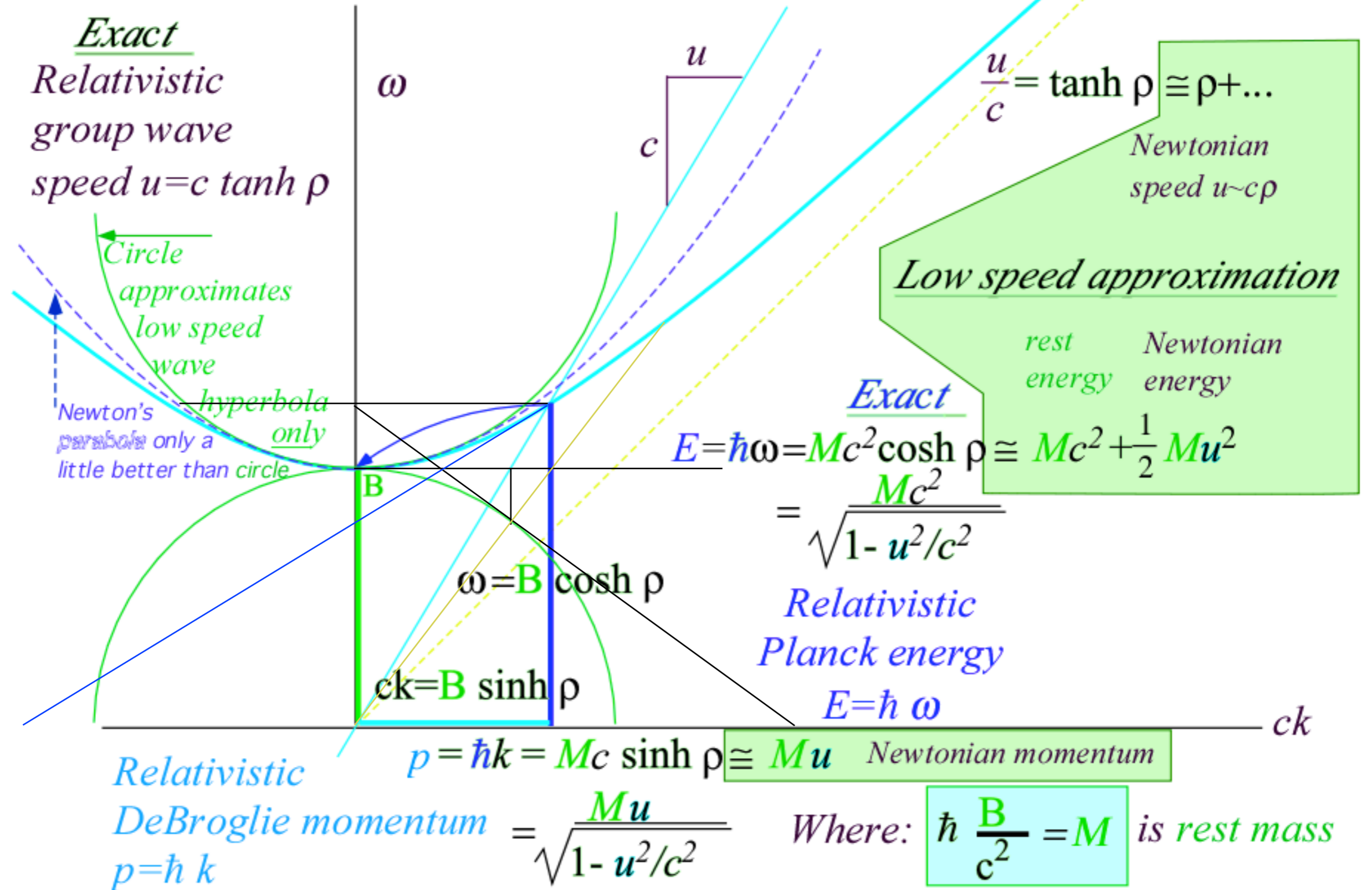
$$= \frac{M u}{\sqrt{1 - u^2/c^2}}$$

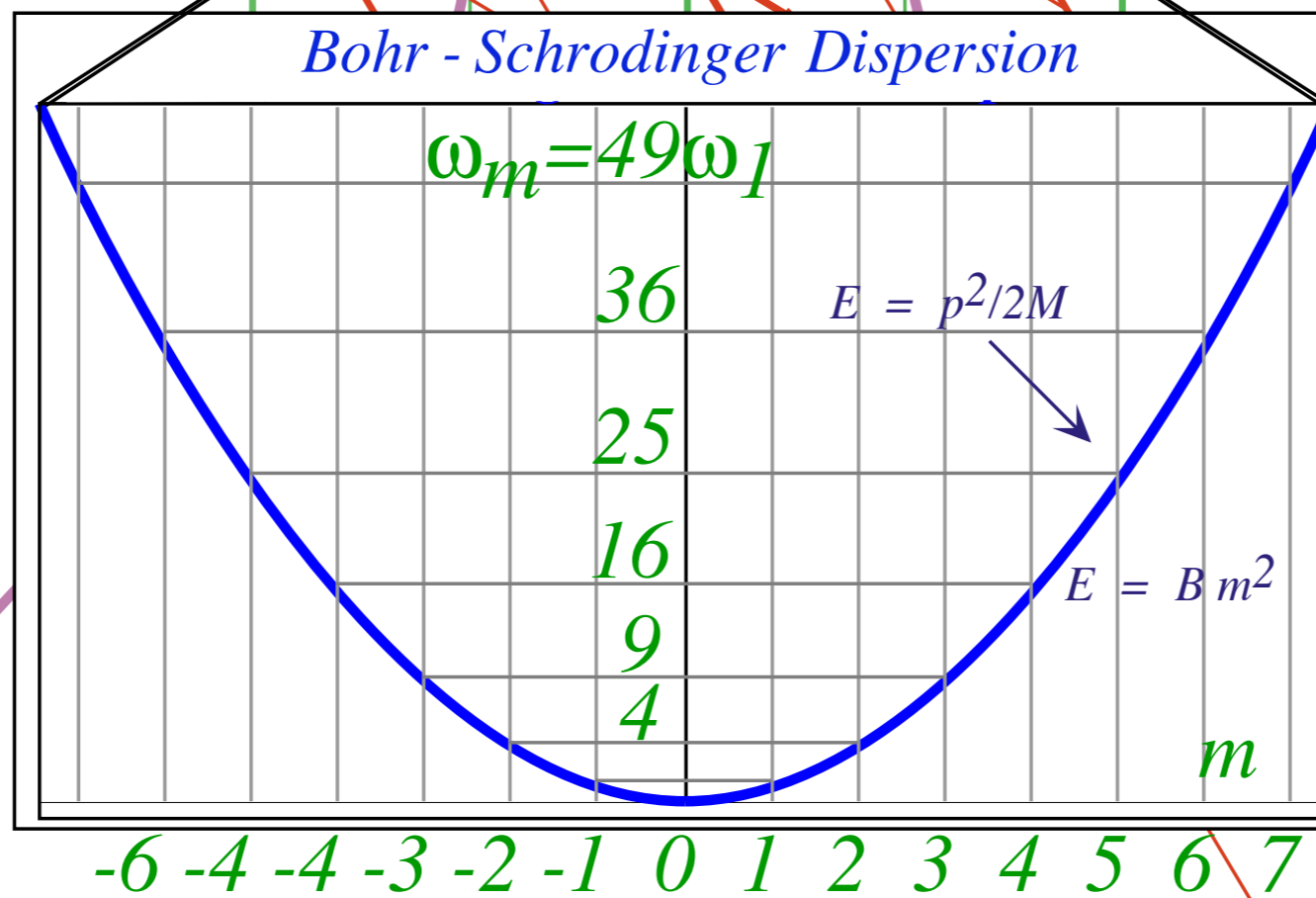
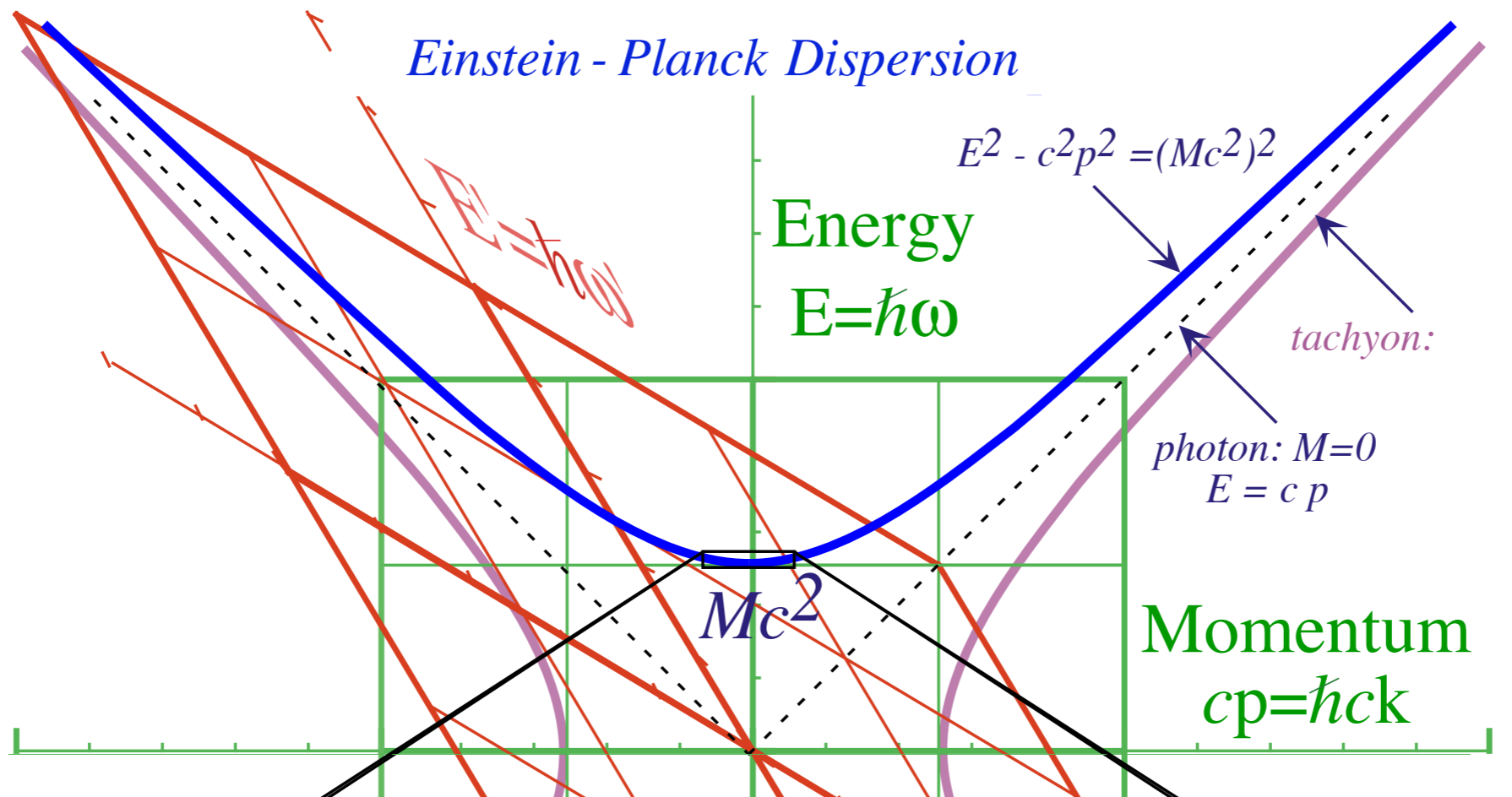
Rest energy ($u=0$): $\hbar \mathbf{B} = M c^2$

Rest momentum ($u=0$): $p=0$

Scale factors determined by experiment
Planck's constant
 $s = \hbar = 1.054572 \cdot 10^{-34} \text{ Joule} \cdot \text{s}$
 $h = 6.626069 \cdot 10^{-34} \text{ J} \cdot \text{s} = 2\pi \hbar$

Summary of geometry ω -vs- ck or E -vs- cp relations with velocity u or rapidity ρ





Relativistic Classical and Quantum Mechanics

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What's the Matter with Mass?

Brief look at Higgs

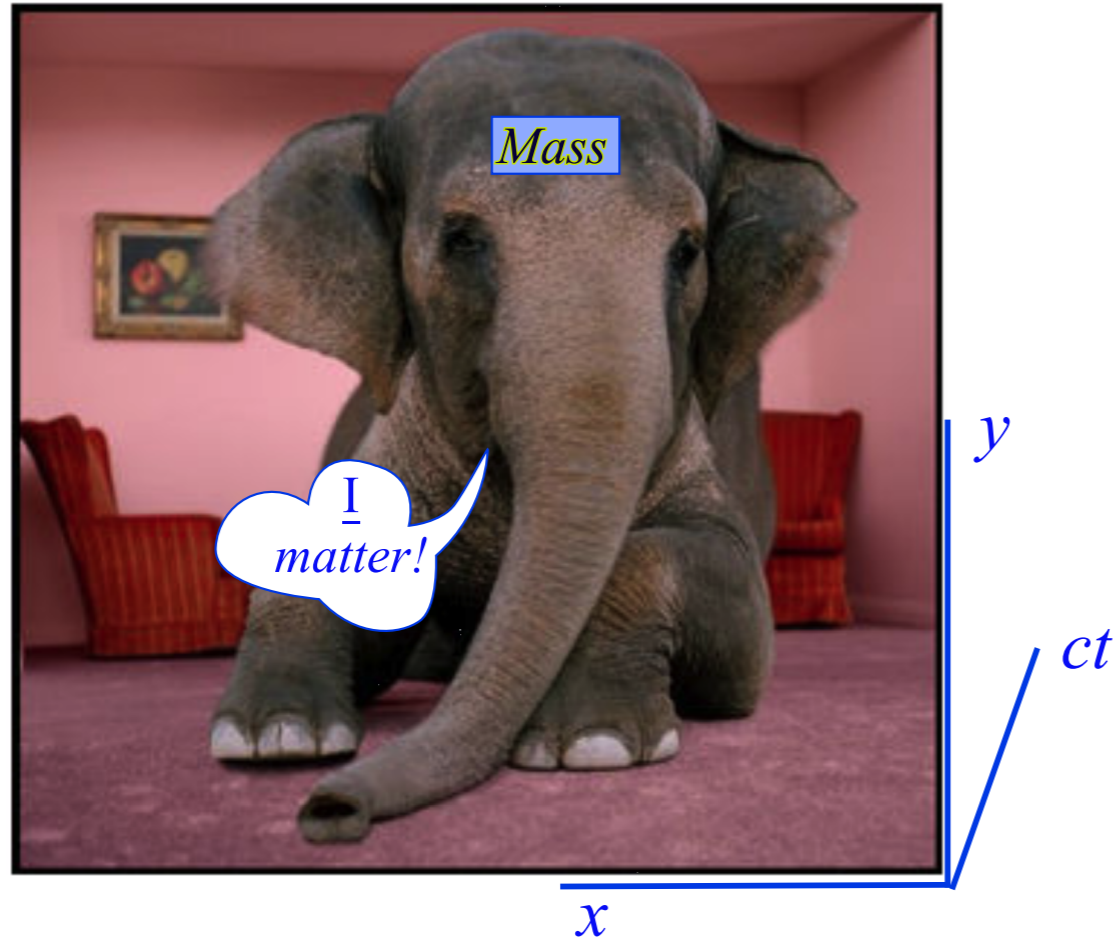
Three kinds of mass (Einstein rest mass, Galilean momentum mass, Newtonian inertial mass)

What's the matter with light?

Bohr-Schrodinger (BS) approximation throws out Mc^2

What's the matter with *Mass*?

Dealing with one of the elephants in the spacetime room:



A brief History of defining Mass M :

1590 Galileo's "impago"

$$M_{\text{Galileo}} = \frac{\text{Momentum}}{\text{Velocity}} = \frac{M \cdot v}{v}$$

1687 Newton's "inertia"

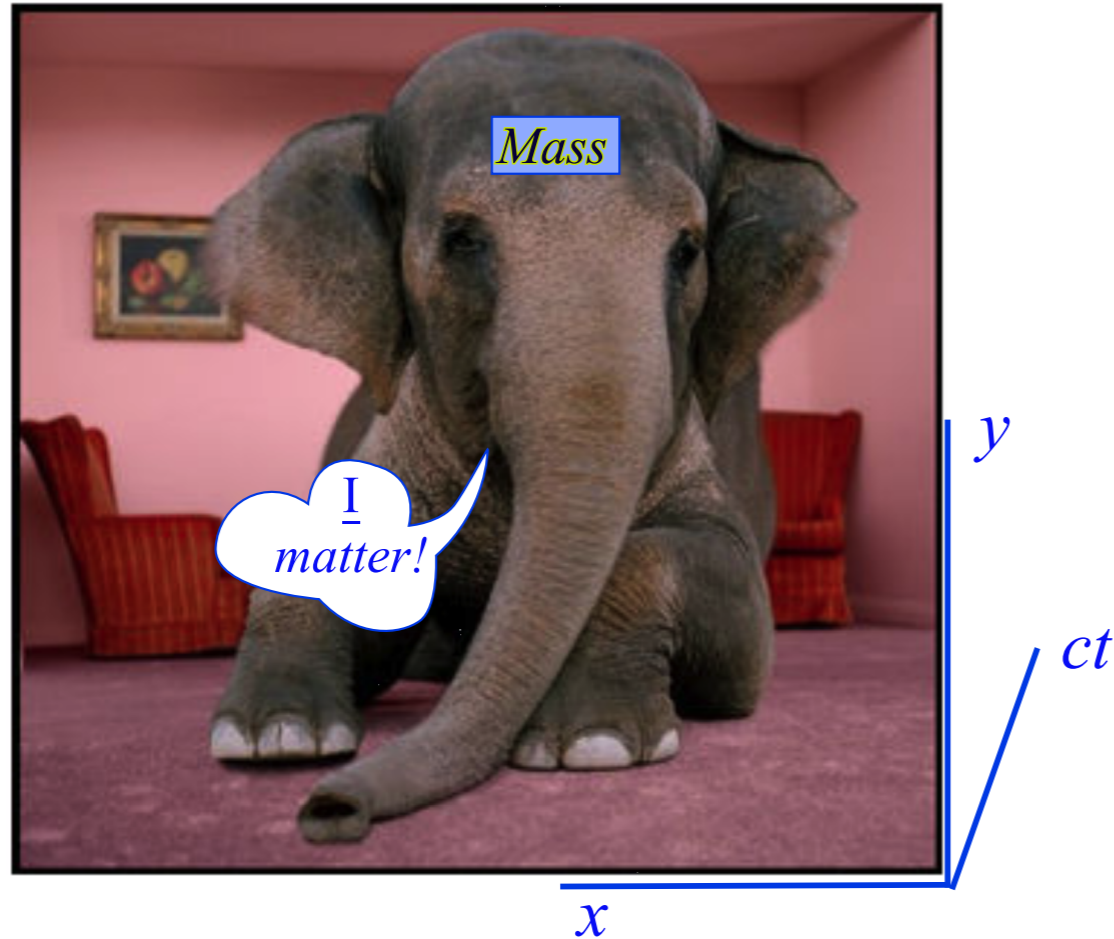
$$M_{\text{Newton}} = \frac{\text{Change in Momentum}}{\text{Change in Velocity}} = \frac{M \cdot a}{a}$$

1905 Einstein's "rest mass"

$$M_{\text{Einstein}} = \frac{\text{Energy}}{(\text{lightspeed})^2} = \frac{M \cdot c^2}{c^2}$$

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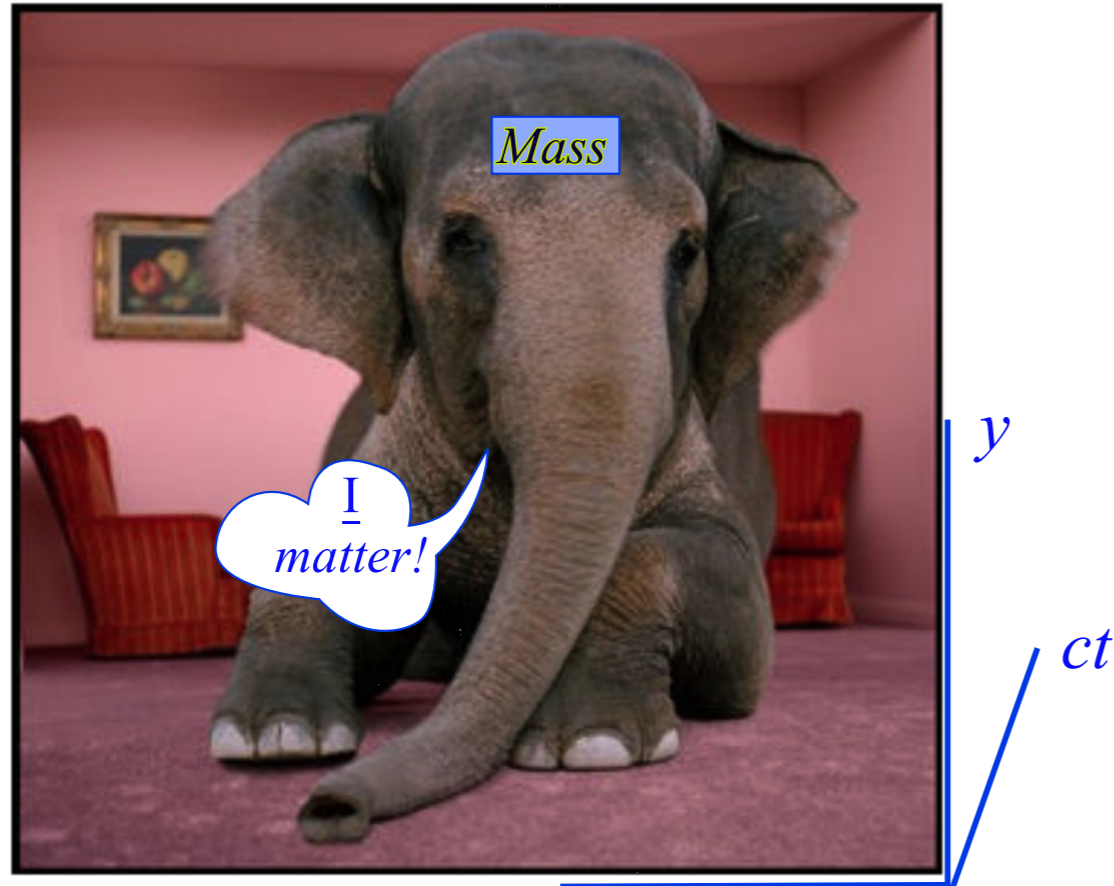
$$M_{\text{Einstein}} = \frac{\text{Energy}}{(\text{lightspeed})^2} = \frac{M \cdot c^2}{c^2}$$

2013 Higgs "Boson"

$$M_{\text{Higgs}} = ? \quad (\text{No simple formula})$$

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$$M_{\text{Higgs}} = ? \quad (\text{No simple formula})$$

News for higgs boson



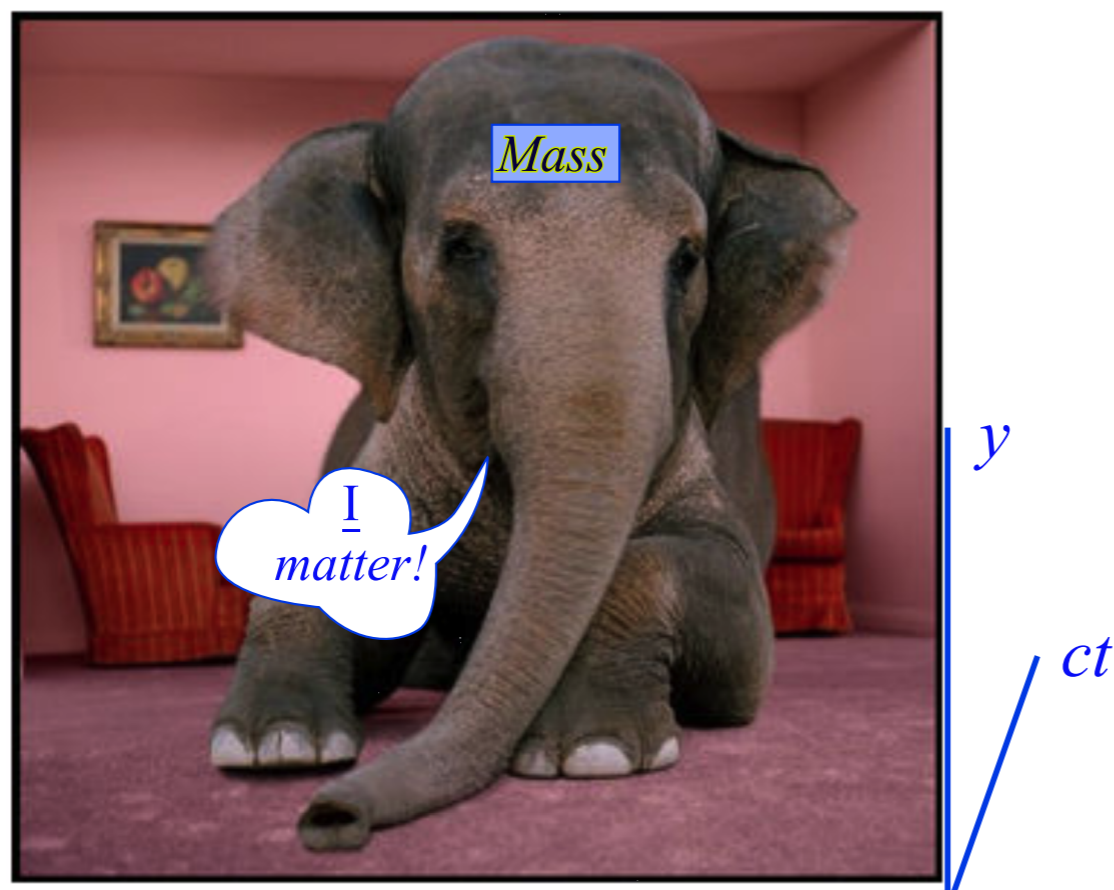
[Working on the 'God particle' saved my life, says Peter Higgs](#)

[The Independent](#) - by Kunal Dutta - 1 day ago

The Nobel prize-winning physicist Peter Higgs has described the fame he has endured since the discovery of his "God particle" as "a bit of a ..."

What's the matter with *Mass*?

Dealing with one of the elephants in the spacetime room:



A brief History of defining Mass M :

1590 Galileo's "impago"

$$M_{\text{Galileo}} = \frac{\text{Momentum}}{\text{Velocity}} = \frac{M \cdot v}{v}$$

1687 Newton's "inertia"

$$M_{\text{Newton}} = \frac{\text{Change in Momentum}}{\text{Change in Velocity}} = \frac{M \cdot a}{a}$$

1905 Einstein's "rest mass"

$$M_{\text{Einstein}} = \frac{\text{Energy}}{(\text{lightspeed})^2} = \frac{M \cdot c^2}{c^2}$$

2013 Higgs "Boson"

$$M_{\text{Higgs}} = ? \quad (\text{No simple formula})$$

News for higgs boson



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[Father of 'the God particle' Peter Higgs says fame is a bit of a nuisance](#)

[The Guardian](#) - 1 day ago

[Professor Higgs Says Fame Is 'A Bit Of A Nuisance' Since Boson's Discovery](#)

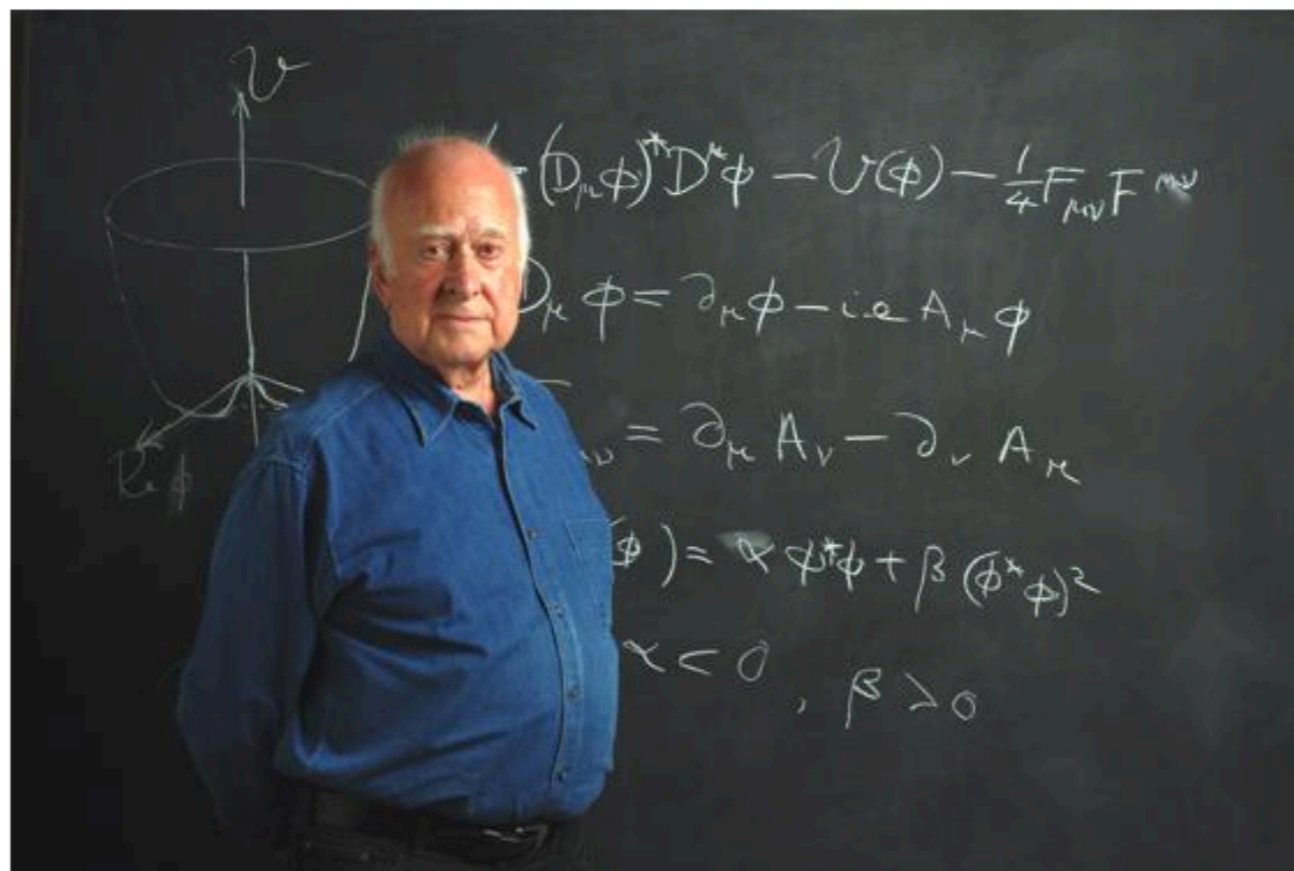
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Peter Higgs and the Higgs Boson

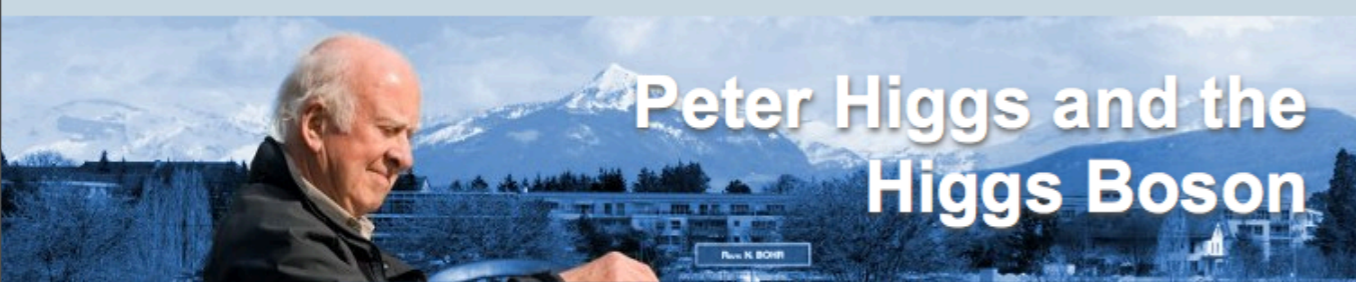
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Peter Higgs and the Higgs Boson



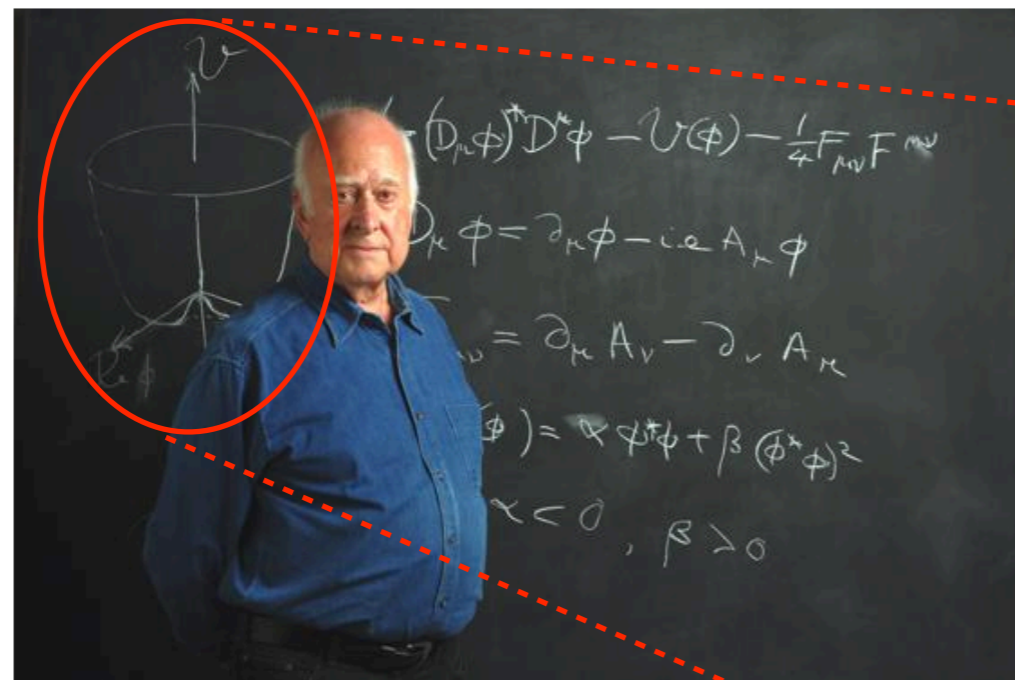
Welcome to the Higgs site at the University of Edinburgh

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Higgs Model based on Molecular Symmetry Stability (Jahn, Teller, Renner, ...)

The electronic eigenstates can be expressed very nicely in terms of the normal coordinate polar angle for the case $r = 0$

$$\begin{aligned}
 |\varepsilon_+\rangle &= \cos(\phi/2) \begin{vmatrix} E \\ 1 \end{vmatrix} - \sin(\phi/2) \begin{vmatrix} E \\ 2 \end{vmatrix}, \\
 |\varepsilon_-\rangle &= \sin(\phi/2) \begin{vmatrix} E \\ 1 \end{vmatrix} + \cos(\phi/2) \begin{vmatrix} E \\ 2 \end{vmatrix}.
 \end{aligned}
 \tag{6.7.9}$$

$E_{1,2}$ -Coordinate Plots

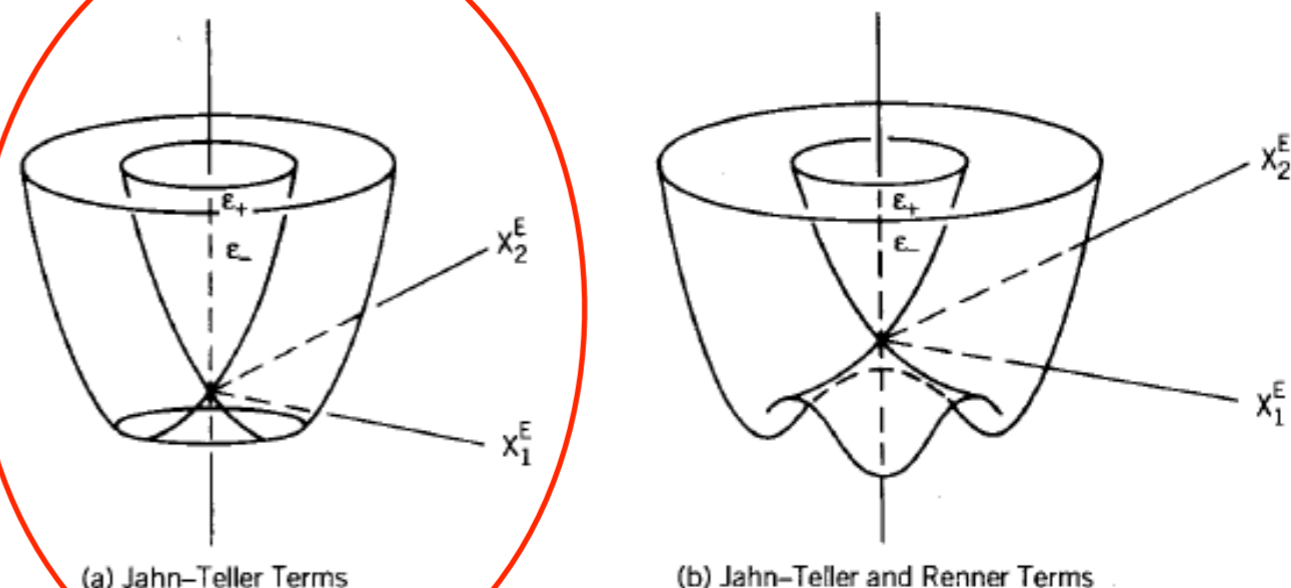


Figure 6.7.1 Potential energy functions of the E -type coordinates. (a) Jahn-Teller terms ($r = 0$). (b) Jahn-Teller and Renner terms ($r > 0$).

Fig. 6.7.1-2
from
Principles of Symmetry, Dynamics and Spectroscopy

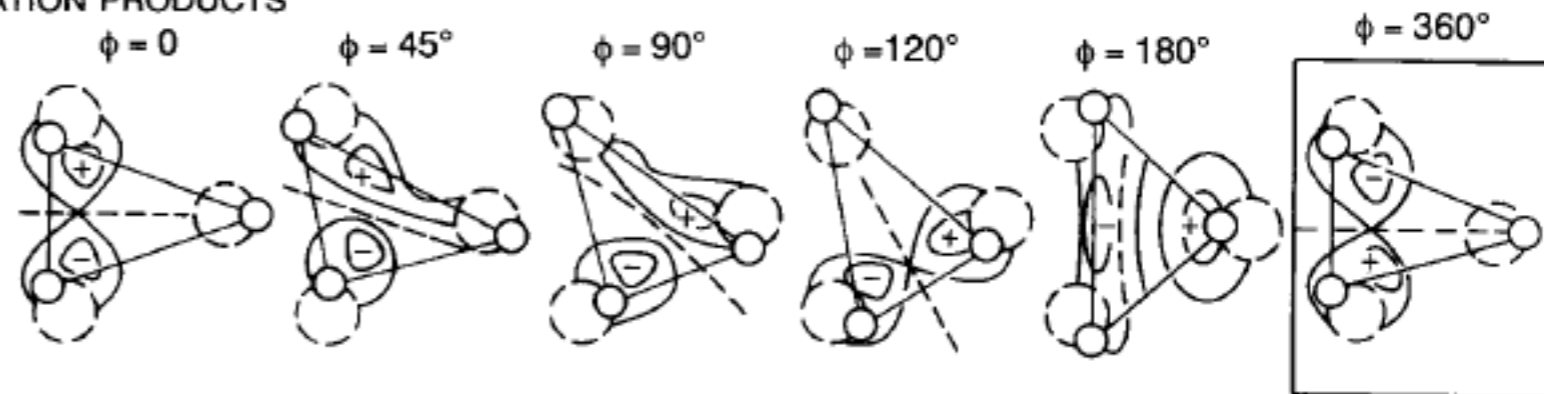


Figure 6.7.2 Electronic state $|\varepsilon_-\rangle$ for various nuclear positions allowed by varying E coordinates.

Relativistic Classical and Quantum Mechanics

How optical CW group and phase properties give relativistic mechanics

What's the Matter with Mass?

Brief look at Higgs

 *Three kinds of mass (Einstein rest mass, Galilean momentum mass, Newtonian inertial mass)*

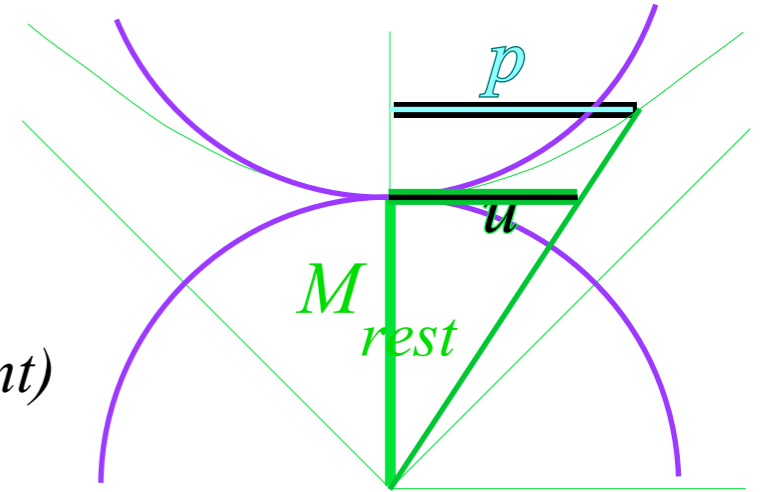
What's the matter with light?

Bohr-Schrodinger (BS) approximation throws out Mc^2

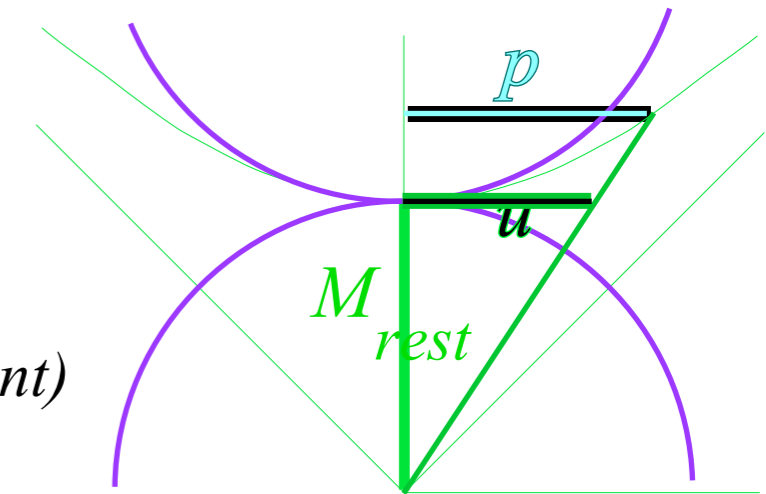
What's the Matter With Light? *Three definitions of "optical mass"*

1. Rest mass $M_N = h\nu_N/c^2$ based on Planck's law $E = h\nu_N = Nh\nu_I$

Rest mass: $M_{rest} = E/c^2 = h\nu_N/c^2$ (Is ρ -invariant)



What's the Matter With Light? *Three definitions of "optical mass"*



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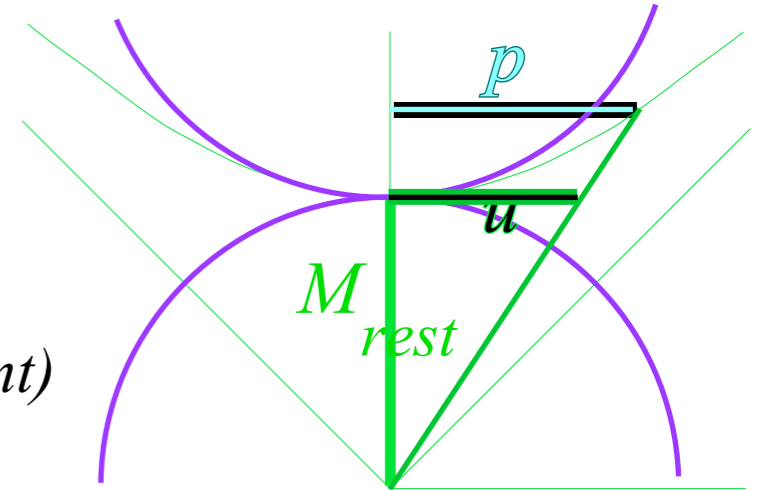
2. *Momentum mass* is defined by Galileo's old formula $p = Mu$ with newer forms for momentum $p = M_{rest} u \cdot \cosh \rho = M_{rest} u / (1 - u^2/c^2)^{1/2}$ and group velocity $u = d\omega/dk$.

It is the ratio p/u of *momentum* to *velocity*.

$$\begin{aligned} \text{Momentum mass: } M_{momentum} &= p/u &= M_{rest} \cosh \rho \\ & &= M_{rest} / (1 - u^2/c^2)^{1/2} \end{aligned}$$

(Not ρ -invariant)

What's the Matter With Light? *Three definitions of "optical mass"*



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$$= M_{rest} / (1 - u^2/c^2)^{1/2}$$

3. *Effective mass* is defined by Newton's old formula $F = Ma$ with newer forms for $F = dp/dt = \hbar dk/dt$ and $a = du/dt =$ to give $F/a = (\hbar dk/dt)(dt/du) = \hbar dk/du = \hbar/(du/dk)$.

It is the ratio F/a of *change of momentum* to the *change of velocity*,

$$\text{Effective mass: } M_{effective} = \hbar/(du/dk) = \hbar/(d^2\omega/dk^2) \quad (\text{Not } \rho\text{-invariant})$$

$$= M_{rest} \cosh^3 \rho = M_{rest} / (1 - u^2/c^2)^{3/2}$$

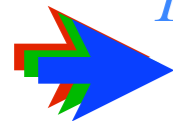
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What's the matter with light?

Three kinds of mass for photon γ in CW relativistic theory

(1) Einstein rest mass

$$M_{rest} = \frac{\hbar\omega_{proper}}{c^2}$$

(2) Galilean momentum mass

$$M_{mom} = p/u = \frac{\hbar k}{\frac{d\omega}{dk}}$$

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$$M_{mom} = F/a = \frac{\hbar}{\frac{d^2\omega}{dk^2}}$$

What's the matter with light?

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$$M_{rest}(\gamma) = 0$$

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$$M_{mom}(\gamma) = p/c = \hbar k/c = \hbar\omega/c^2$$

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$$M_{eff} = F/a = \frac{\hbar}{\frac{d^2\omega}{dk^2}}$$

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Equations (4.11) in Unit 8

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A 2-CW 600THz cavity has zero total momentum p , but each photon adds a tiny mass M_γ to it.

$$M_\gamma = \hbar\omega/c^2 = \omega (1.2 \cdot 10^{-51}) \text{kg} \cdot \text{s} = 4.5 \cdot 10^{-36} \text{kg} \quad (\text{for: } \omega = 2\pi \cdot 600 \text{THz})$$

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A 1-CW state has no rest mass, but 1-photon momentum is a non-zero value $p_\gamma = M_\gamma c$. (*Galilean revenge II.*)

$$p_\gamma = \hbar k = \hbar\omega/c = \omega (4.5 \cdot 10^{-43}) \text{kg} \cdot \text{m} = 1.7 \cdot 10^{-27} \text{kg} \cdot \text{m} \cdot \text{s}^{-1} \quad (\text{for: } \omega = 2\pi \cdot 600 \text{THz})$$

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$$E = \frac{Mc^2}{\sqrt{1 - u^2/c^2}} = Mc^2 \cosh \rho = Mc^2 \sqrt{1 + \sinh^2 \rho} = \sqrt{(Mc^2)^2 + (cp)^2}$$

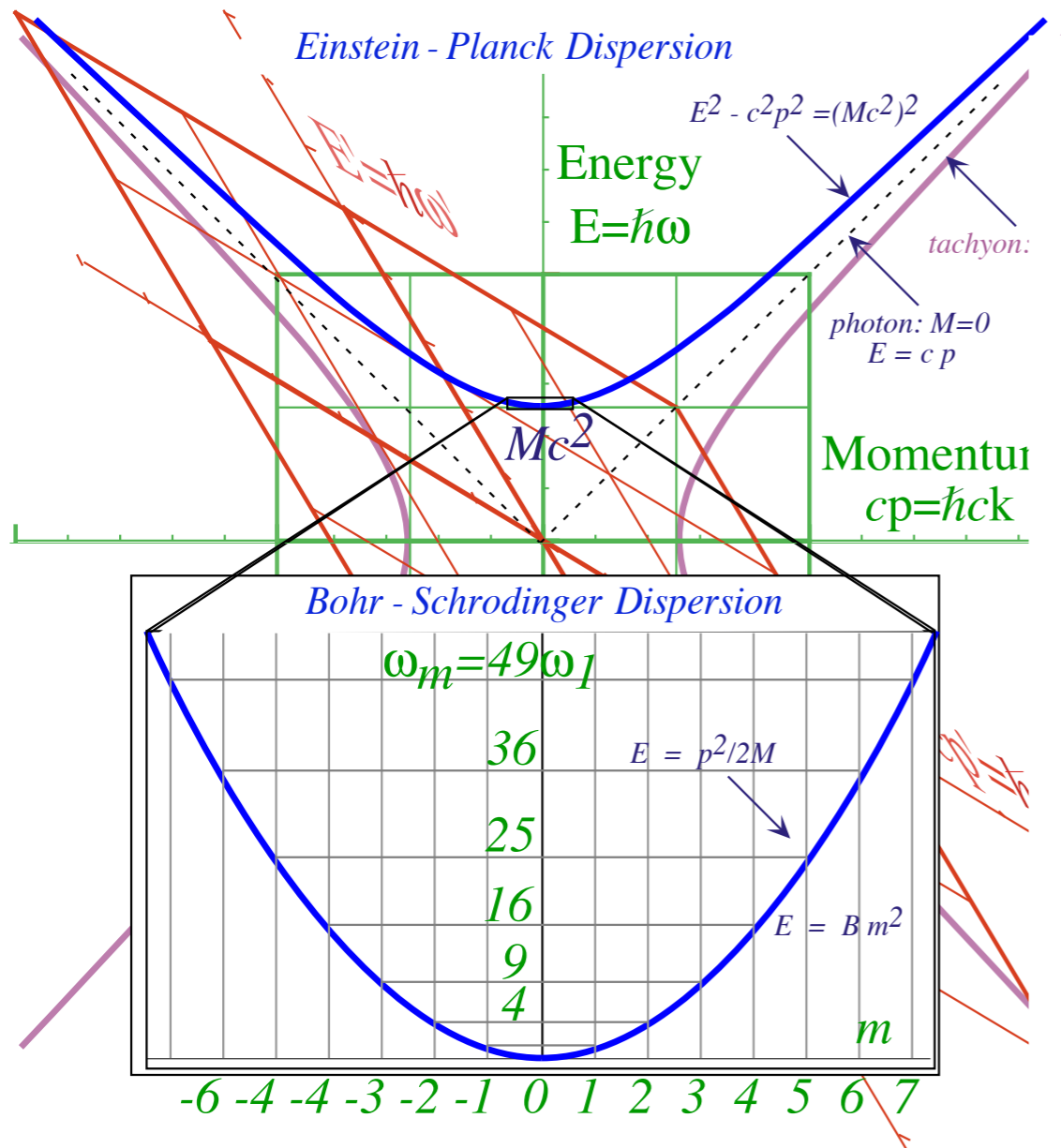
$$E = \left[(Mc^2)^2 + (cp)^2 \right]^{1/2} \approx Mc^2 + \frac{1}{2M} p^2 \xrightarrow{\text{BS-approx}} \frac{1}{2M} p^2$$

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The BS claim: may shift energy origin ($E=Mc^2, cp=0$) to ($E=0, cp=0$). (Frequency is relative!)

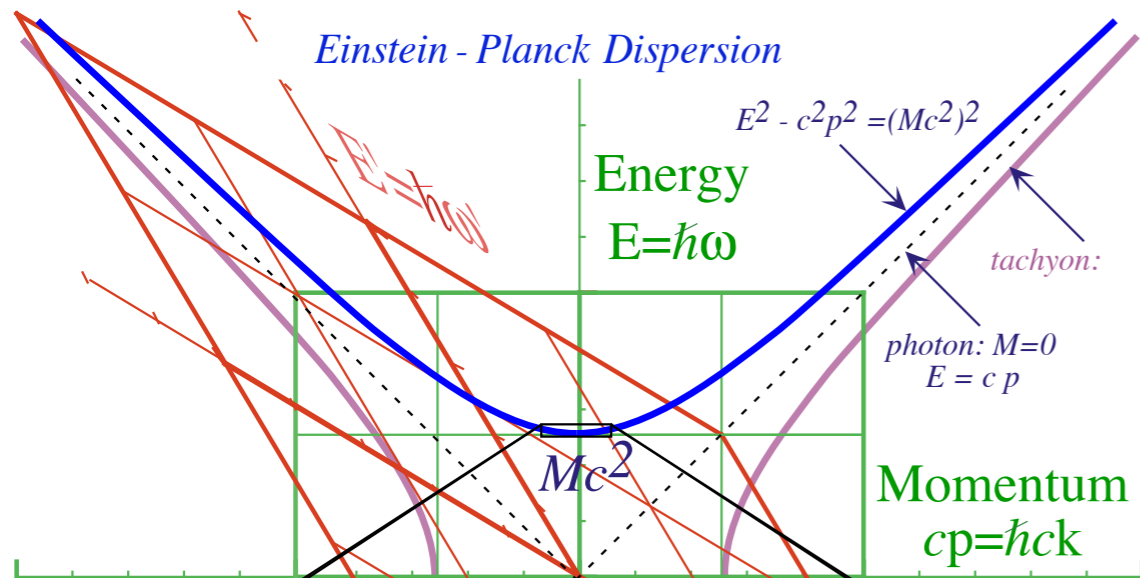


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Group velocity $u = V_{group} = \frac{d\omega}{dk}$ is a differential quantity unaffected by origin shift.

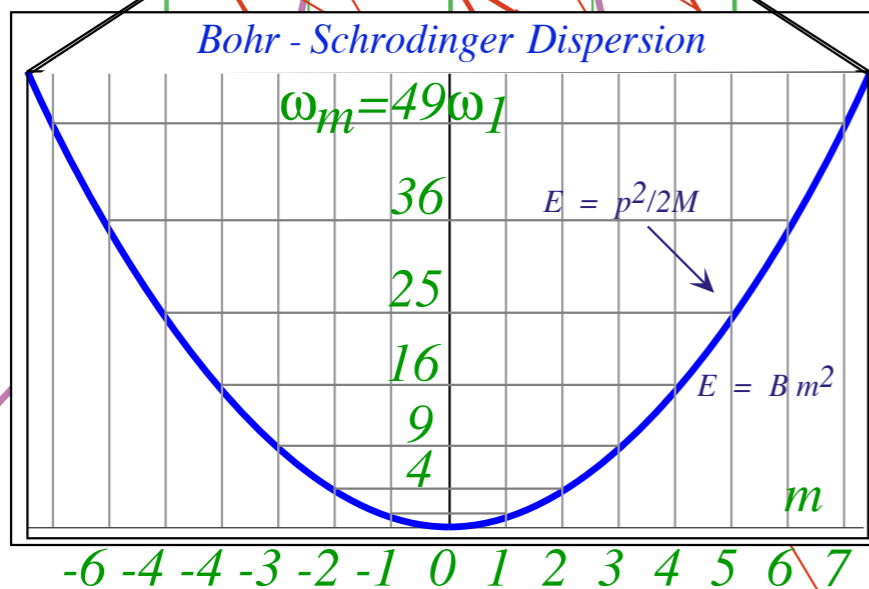
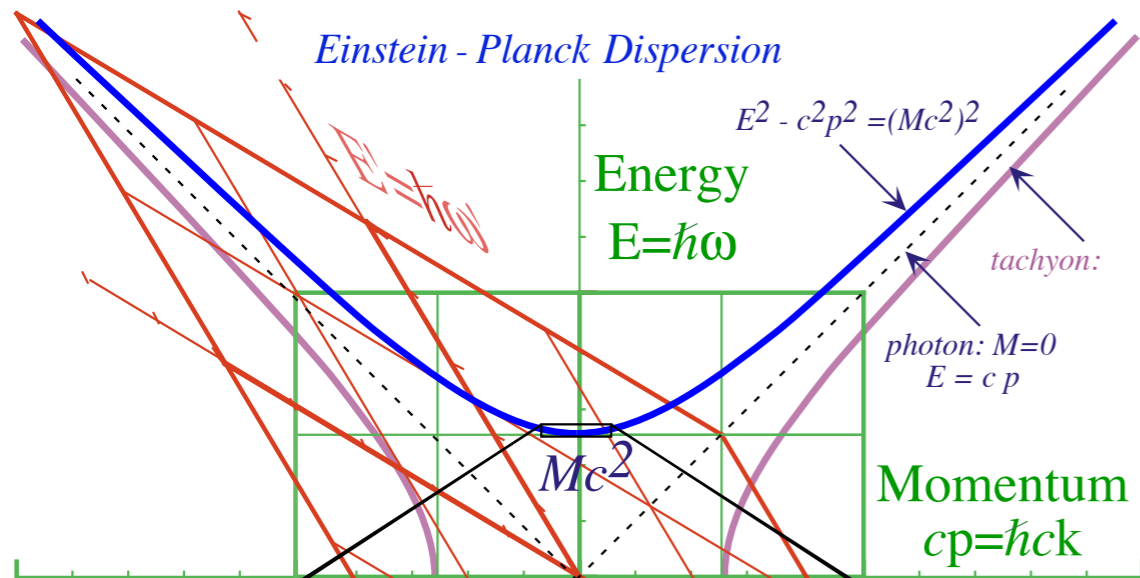
But, Phase velocity $\frac{\omega}{k} = V_{phase}$ is greatly reduced by deleting Mc^2 from $E = \hbar\omega$.

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But, Phase velocity $\frac{\omega}{k} = V_{phase}$ is greatly reduced by deleting Mc^2 from $E = \hbar\omega$.

It slows from $V_{phase} = c^2/u$ to a sedate sub-luminal speed of $V_{group}/2$.

$$\omega_{BS}(k) = \frac{k^2}{2M} \quad \text{gives:} \quad V_{phase} = \frac{\omega_{BS}}{k} = \frac{k}{2M}$$

$$\text{and:} \quad V_{group} = \frac{d\omega_{BS}}{dk} = \frac{k}{M}$$

